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**TECHNOLOGICAL**  
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# **Statistics for Proteomics**

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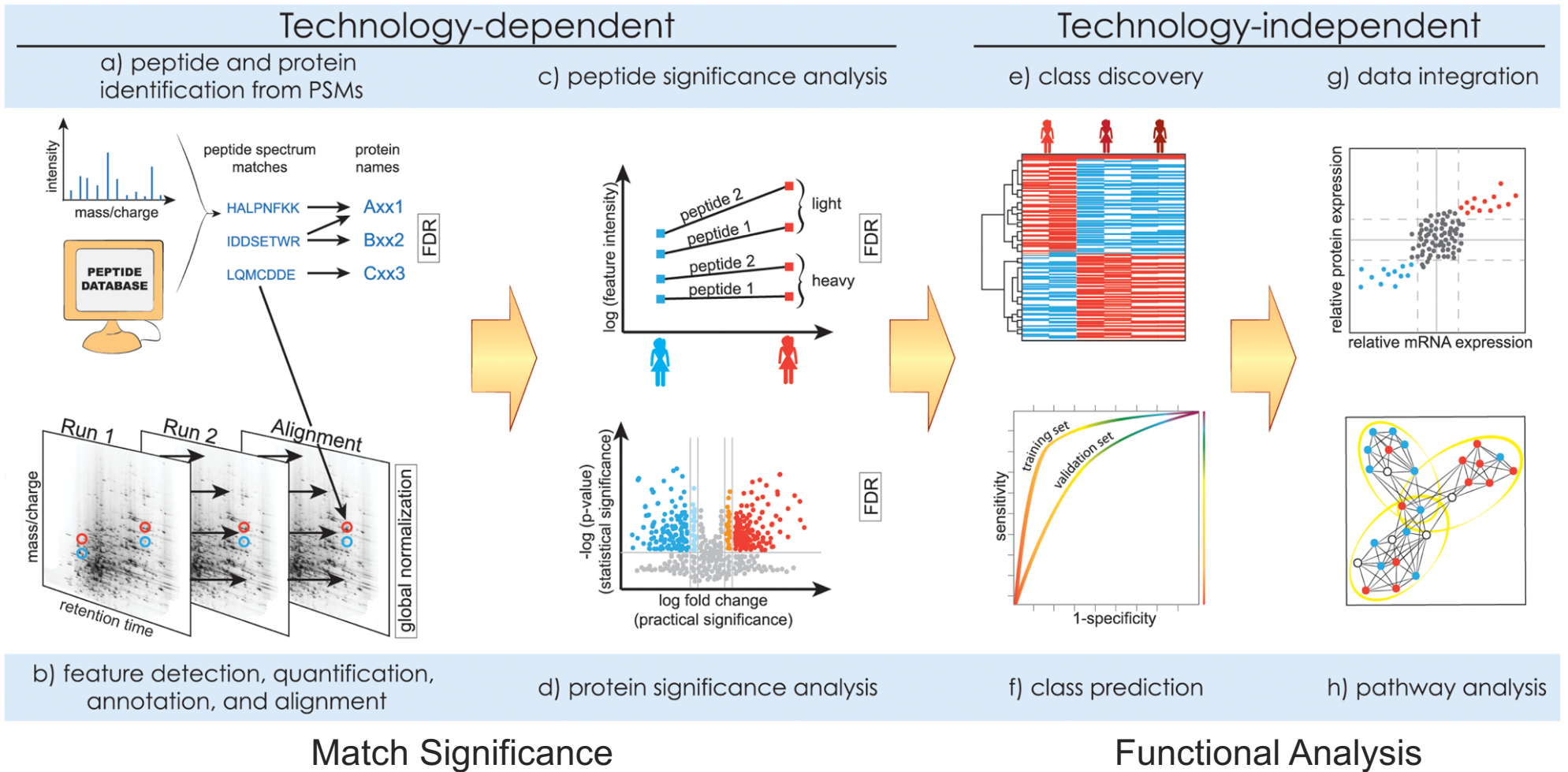
*School of Biological Sciences, Nanyang Technological University*

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# Learning objectives

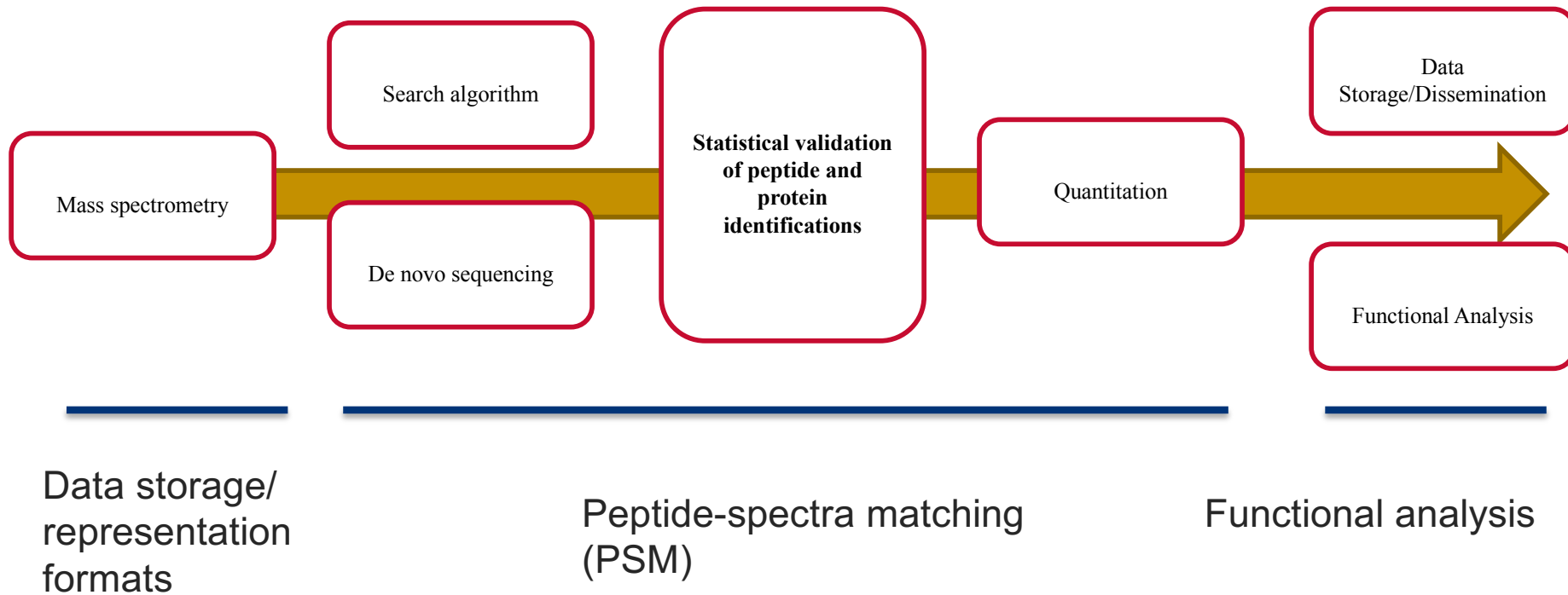
- Describe the various factors affecting PSM quality
- Describe p-values, FDR and PEP
- Describe and evaluate the various decoy library generation strategies (sequence reversal, sequence randomization) for FDR estimation
- Describe coverage and consistency issues in proteomics

# Using Proteomics in practical applications



Statistics plays key roles in both areas

# Overview of proteo-informatics





# What is PSM?

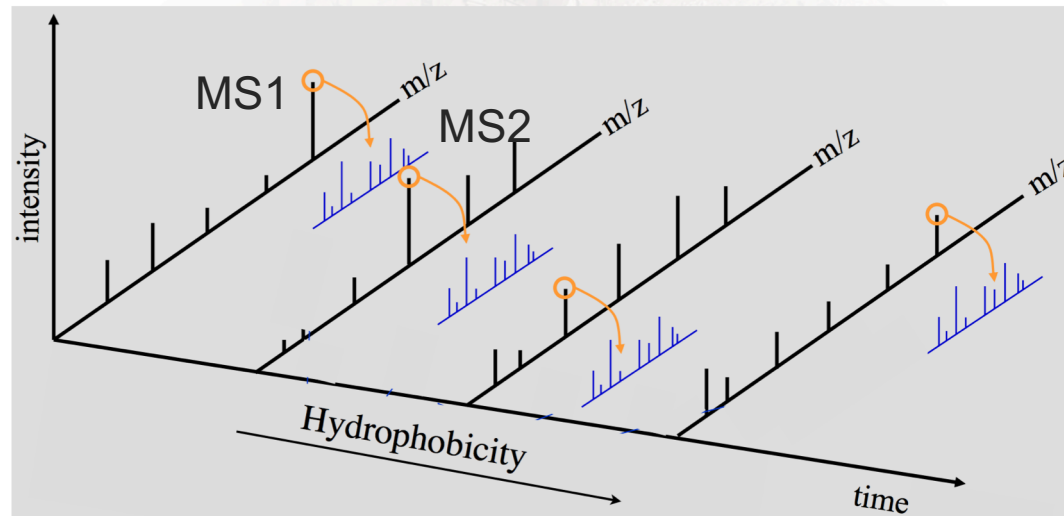
- PSM stands for Peptide-Spectra Match
- It is a pairing of sequence with spectra
- You've seen this earlier when we considered library search algorithms
- Earlier we showed a simple scenario where there is only one possible sequence match per spectra ...
- But in practice ...

# What determines whether or not we get a good PSM?

- Search parameters
- Library quality and size
- Spectra quality
- Algorithm scoring method
- Statistical evaluation

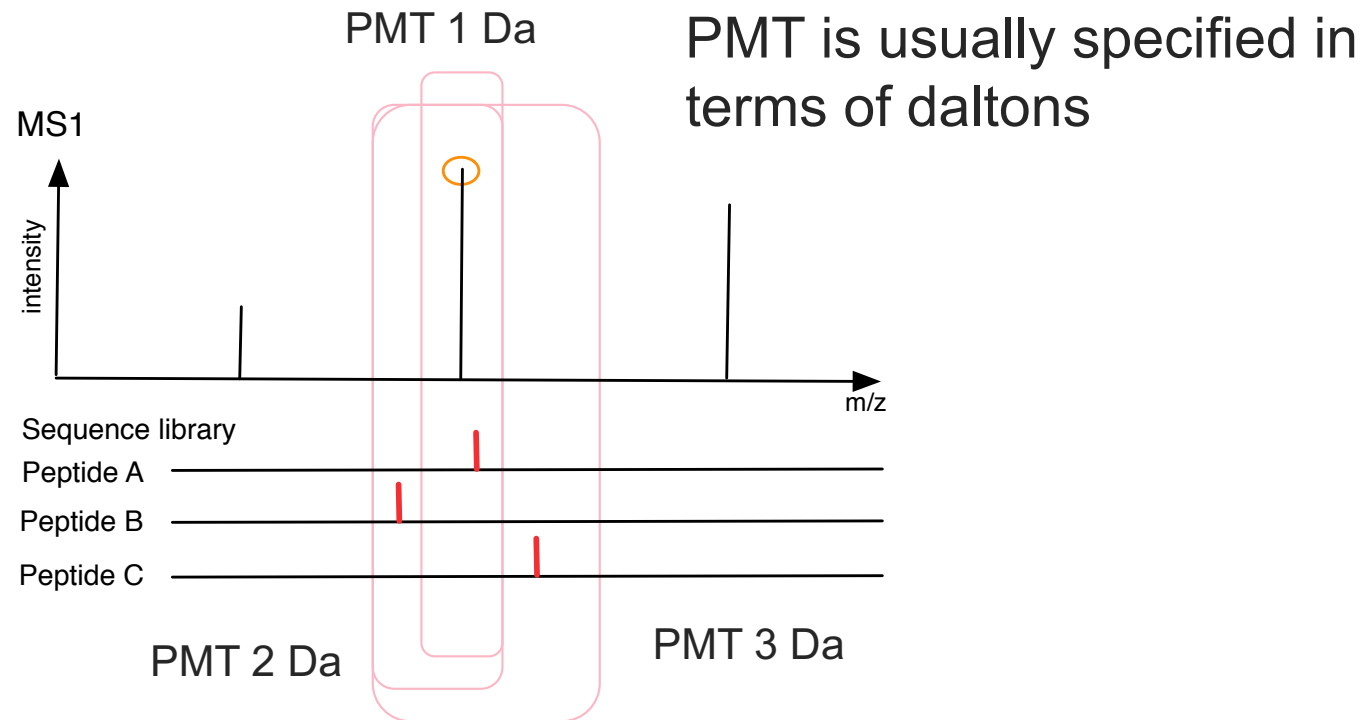
# Search parameters

- Precursor mass tolerance (PMT)
- Fragment mass tolerance (FMT)
- Post-translational modification (PTM)



# Precursor mass tolerance (PMT)

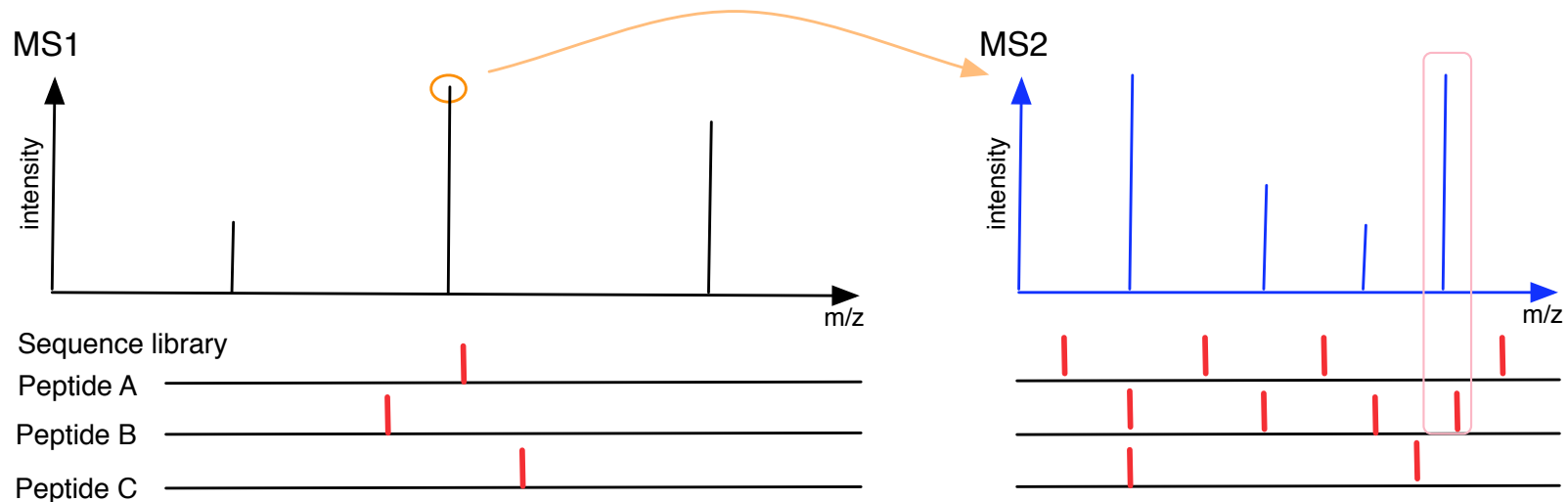
- PMT deals with MS1 (peptide level)



What happens when the PMT window size is increased?

# Fragment mass tolerance (FMT)

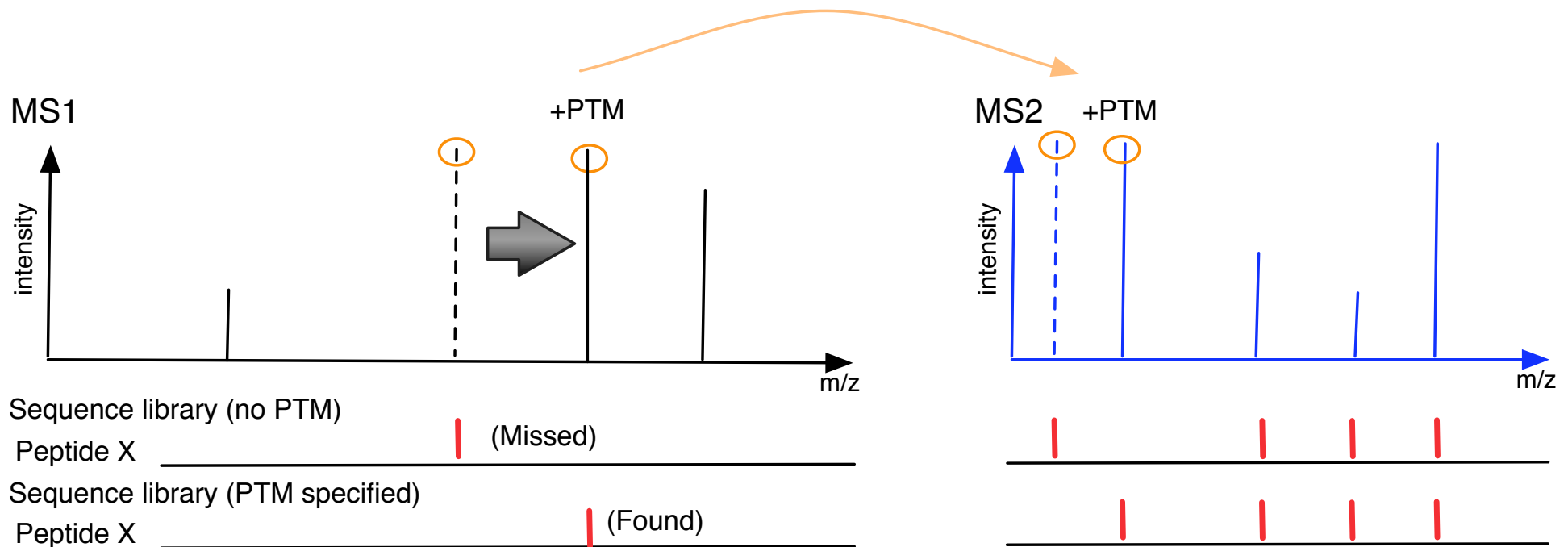
- FMT deals with MS2 (identification level)



Which looks like the correct answer?

# Post-translational modification (PTM)

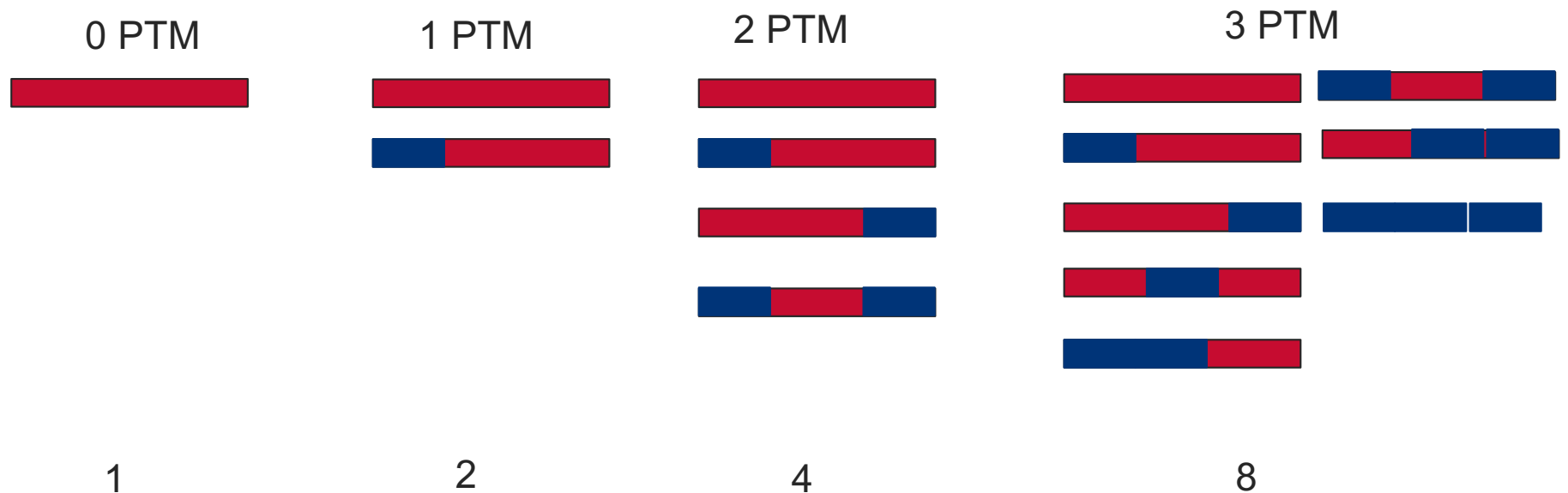
- Some peptide sequences undergo chemical modifications resulting in mass shifts
- If the PTMs are not specified in the search space, then the corresponding PSM may not be detectable



Some fragments will contain the PTM in MS2

# Search space

- The set of candidate peptides to be considered for potential match to spectra
- Without PTMs, the search space is simply the set of peptides
- With PTMs, the search space effectively doubles for every PTM to be considered.



# Examples of typical PTMs

- Phosphorylation
- Ubiquitination
- O-GlcNAcylation
- Methylation
- Acetylation
- Succinylation
- SUMOylation
- Citrullination

Some 260 000 PTM sites that have been identified in the human proteome thus far, but only a few have been assigned to key regulatory and/or other biological roles!

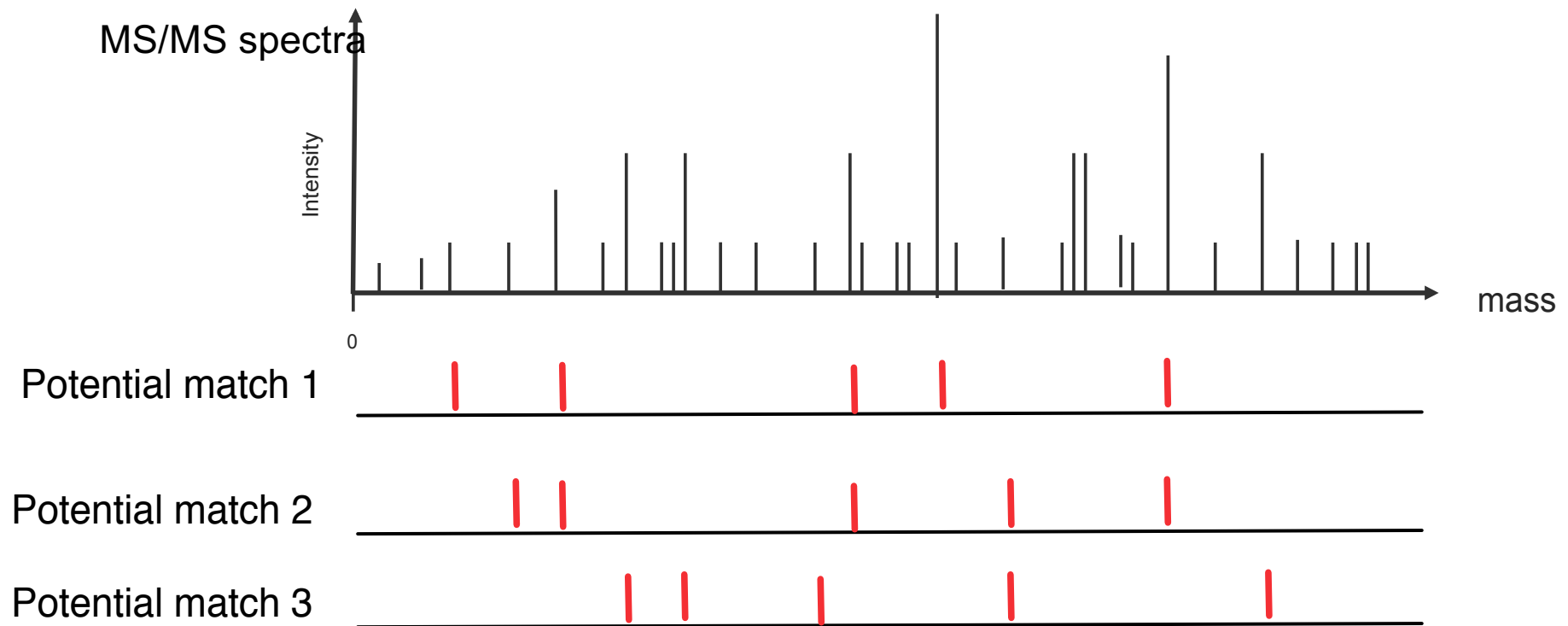
It is difficult to pin-point exact locations of PTMs as well. And incorporating all possibilities (where there is only 1 or few right matches)... can lead to high false positive rates (we will see how later).



# Library quality and size

- UniProt sequence library has 2 databases
  - SwissProt (manually curated and reviewed) -  
> 500K sequences
  - TrEMBL (Automatic annotation, no review) -  
> 90M sequences

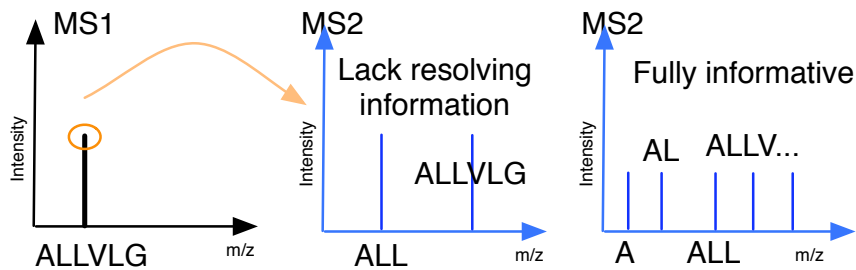
# Consider this scenario...



What are potential explanations for 1, 2 and 3?

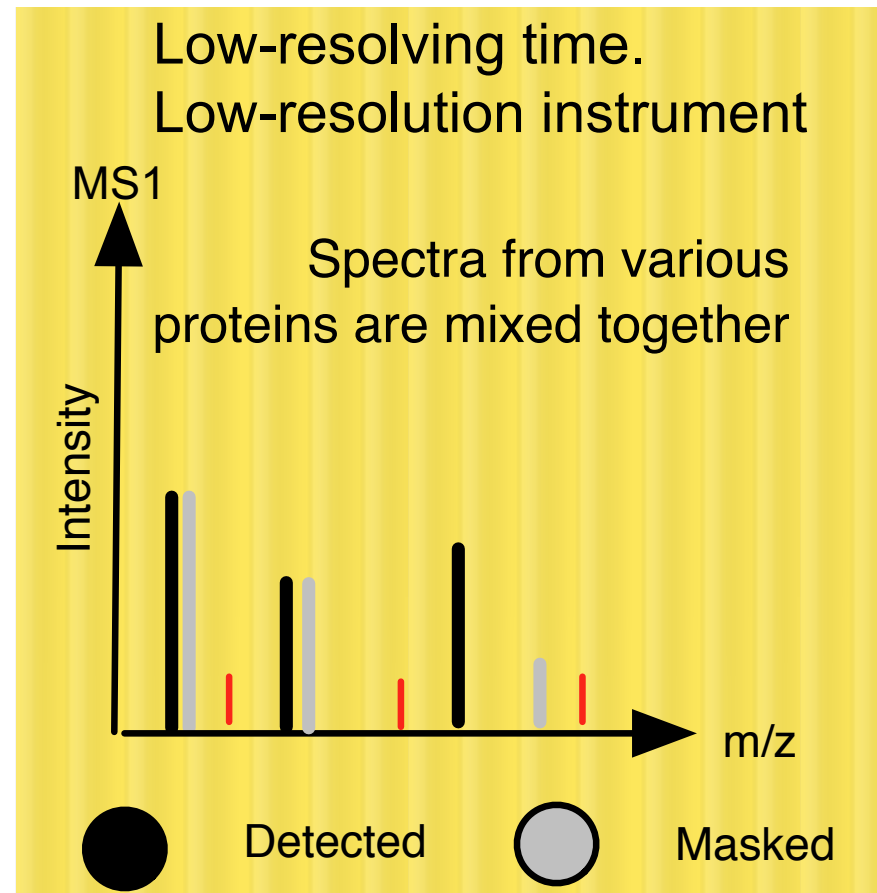
# Spectra Quality

## Incomplete fragmentation



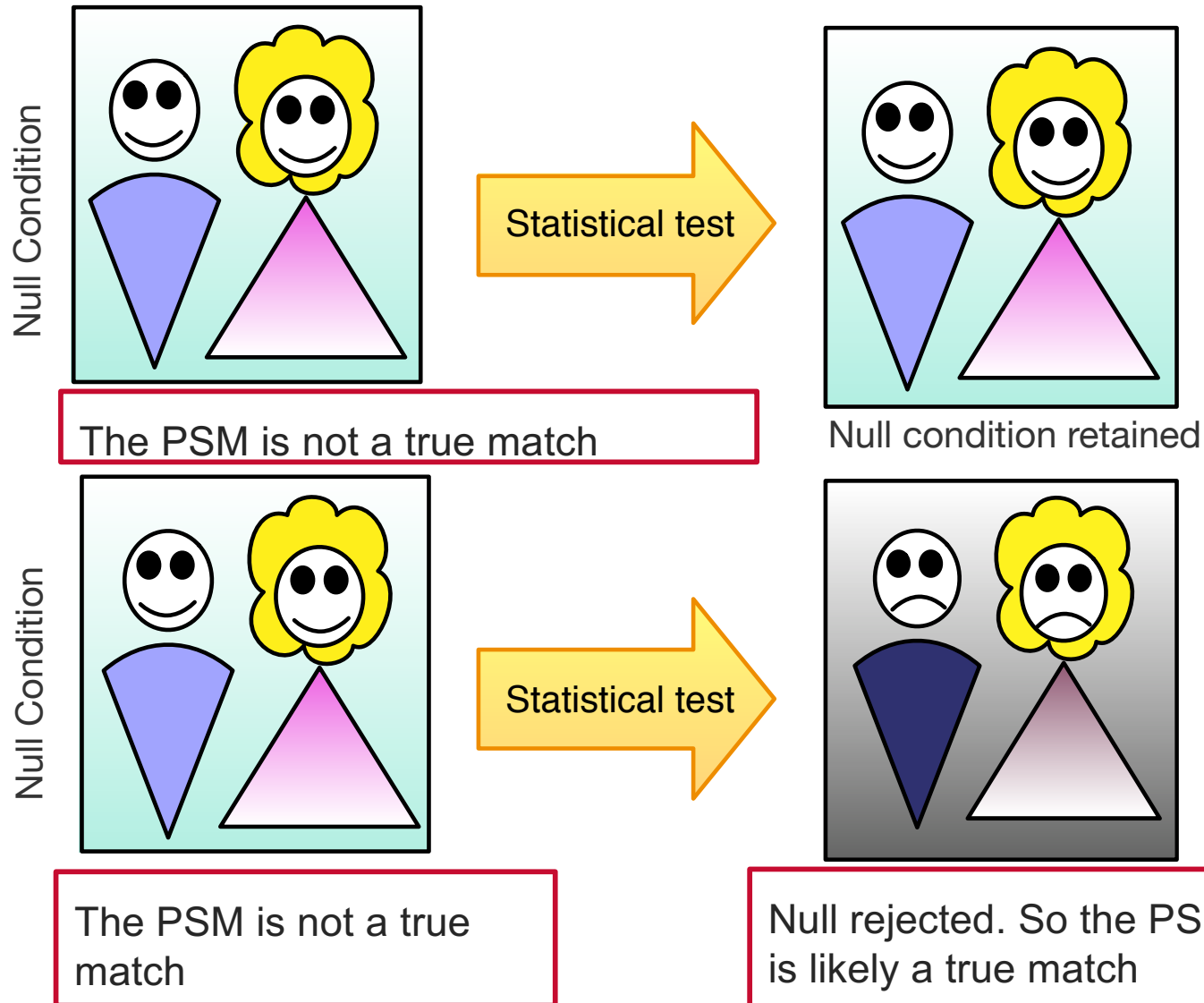
Complete MS2 profile allows confident identification of spectra

## Mixed signals

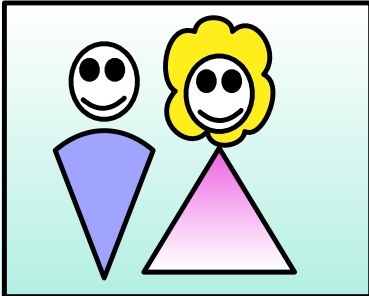
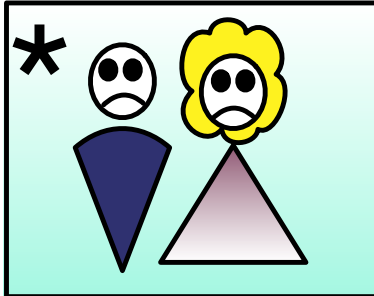
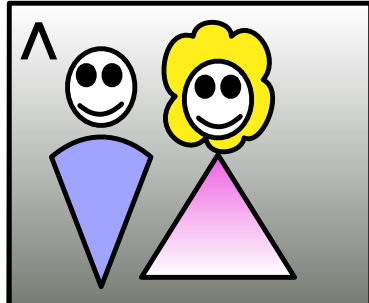
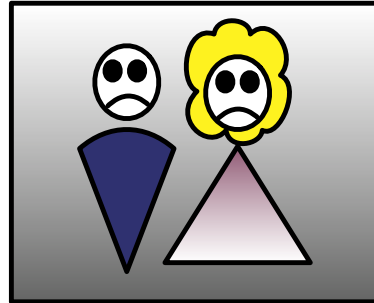


# Statistical testing

## The elements of null hypothesis statistical testing

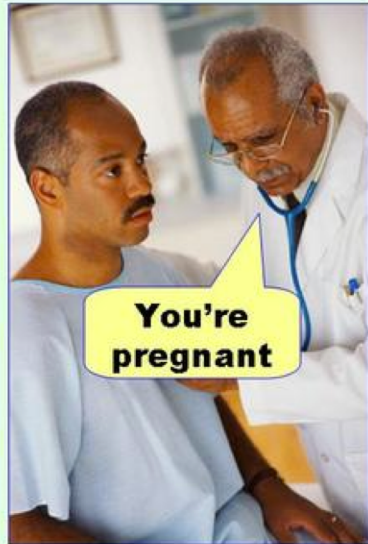


# Possible outcomes from a statistical test

4 Possible outcomes		Predicted as	
		Happy (Irrelevant)	Unhappy (Relevant)
Reality	Happy (Irrelevant)	 <p>True Negative</p>	 <p>False Positive</p>
	Unhappy (Relevant)	 <p>False Negative</p>	 <p>True Positive</p>

# How to remember?

**Type I error**  
(false positive)



**Type II error**  
(false negative)



Do you recall type I and II statistical errors?

Type I: Reject the null when the null is true  
Type II: Fail to reject the null when the null is not true

True positive



True negative



# Possible outcomes given the PSMs

The PSM is...

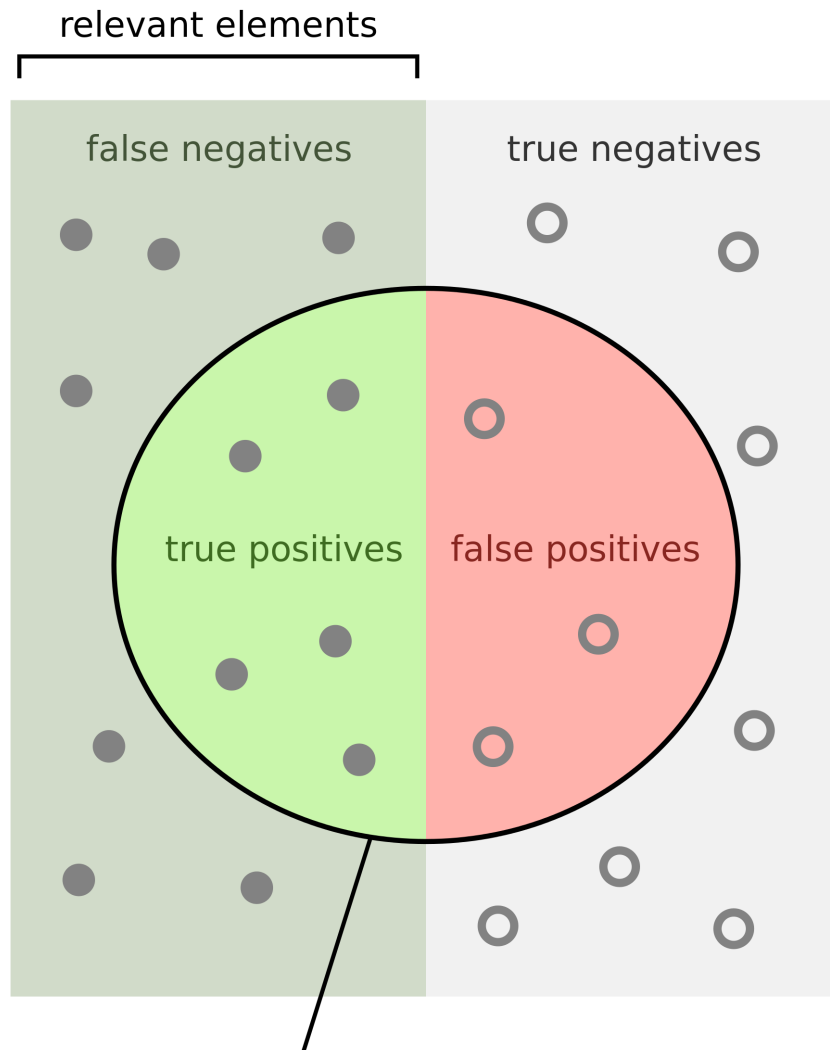
Predicted as

BUT IN  
Reality..

	CORRECT	WRONG
CORRECT		
WRONG		

Imagine we do this for every spectra...

# Recall, Precision and the F-score



selected elements

e.g. let's say we set a p-value cutoff of 0.05

How many selected items are relevant?

$$\text{Precision} = \frac{\text{true positives}}{\text{true positives} + \text{false positives}}$$

How many relevant items are selected?

$$\text{Recall} = \frac{\text{true positives}}{\text{true positives} + \text{false negatives}}$$

Precision: Of the selected feature, How many are correct?

Recall: Of the selected feature, What is the proportion of all the correct ones we got?

Precision and recall can be combined as:

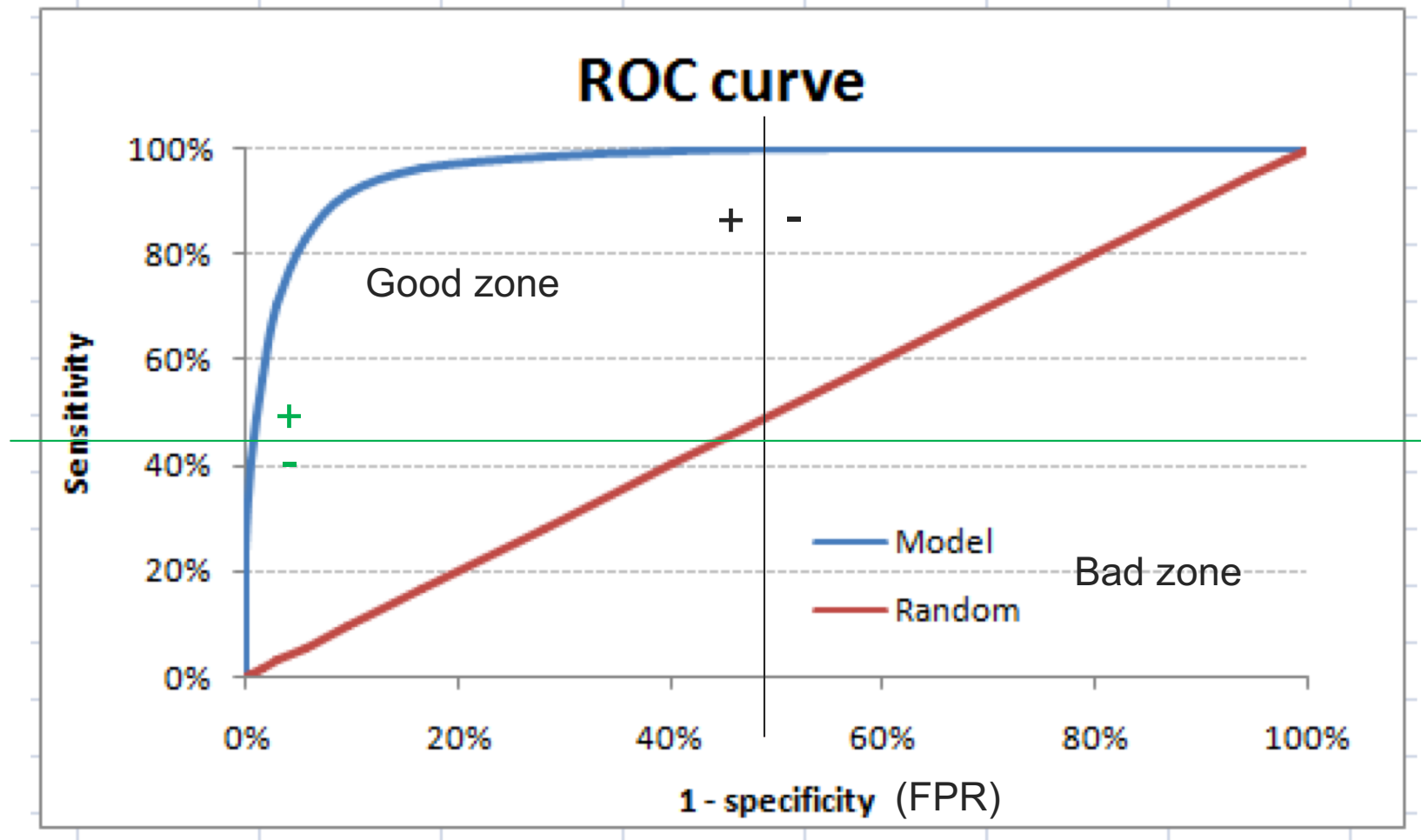
$$F_1 = 2 \cdot \frac{\text{precision} \cdot \text{recall}}{\text{precision} + \text{recall}}$$

Recall is also often called sensitivity or True positive rate



# Precision and recall works against each other

# The Receiver Operator Characteristic (ROC) curve

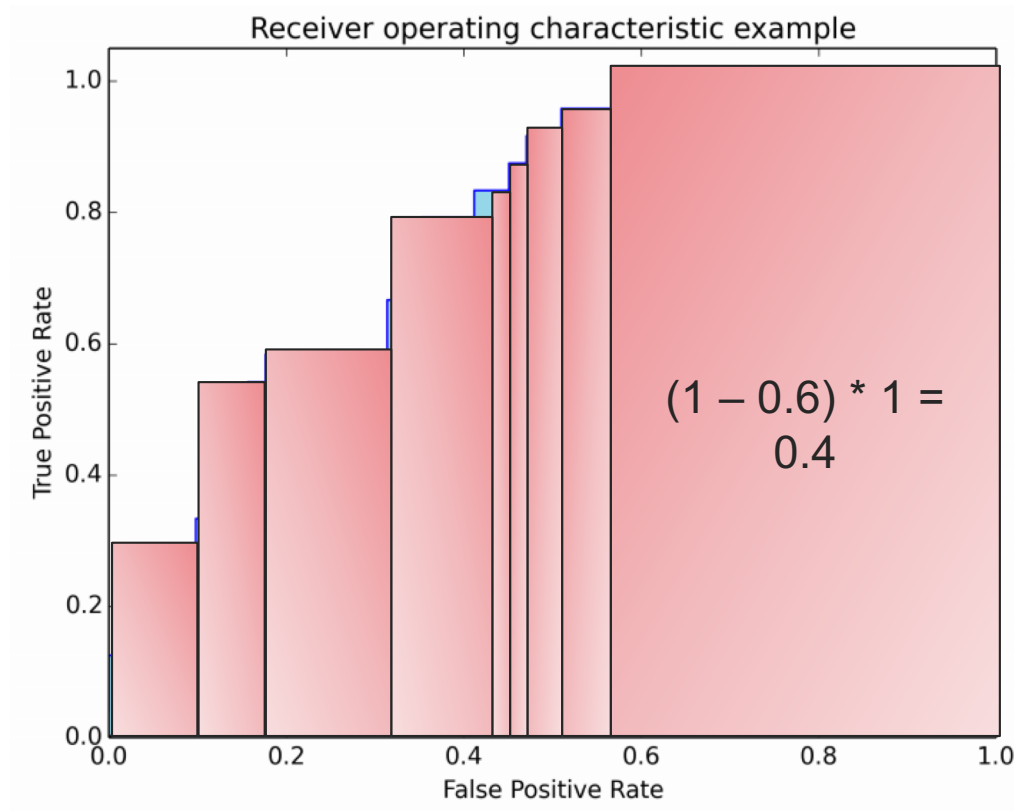


$$\text{specificity} = \frac{\text{number of true negatives}}{\text{number of true negatives} + \text{number of false positives}}$$

Can you write down the formula for FPR yourself?

# The Area Under Curve (AUC)

More rightfully called AUROC (Area under the ROC curve)



The blue area corresponds to the AUROC. The dashed line in the diagonal is expected performance due to random chance (so we have to be better than chance)

Total area =  $1 \times 1 = 1$

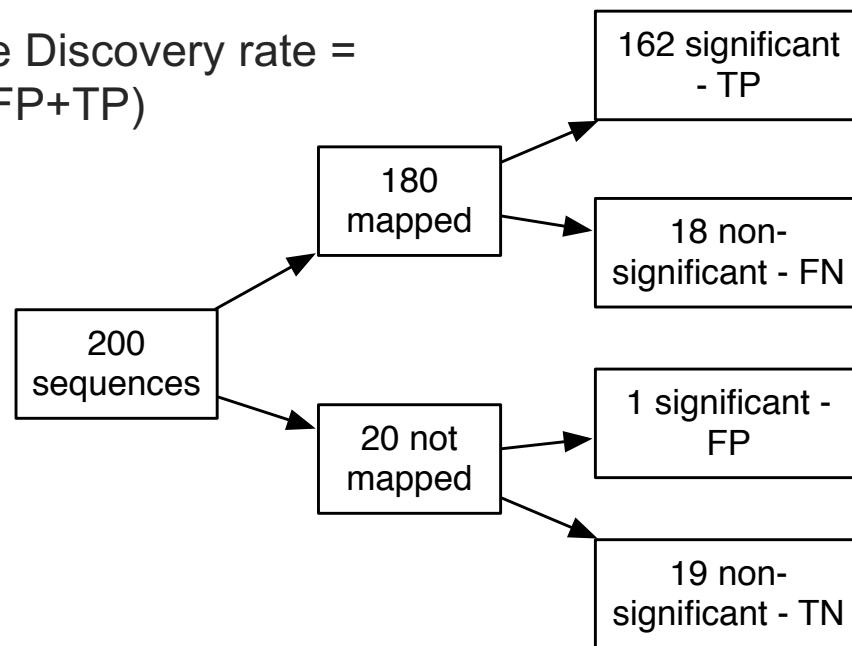
Half area under the diagonal =  $\frac{1}{2} = 0.5$

One simple way to get the AUROC is to simply calculate the area using simple length x breadth. But of course one may use calculus.

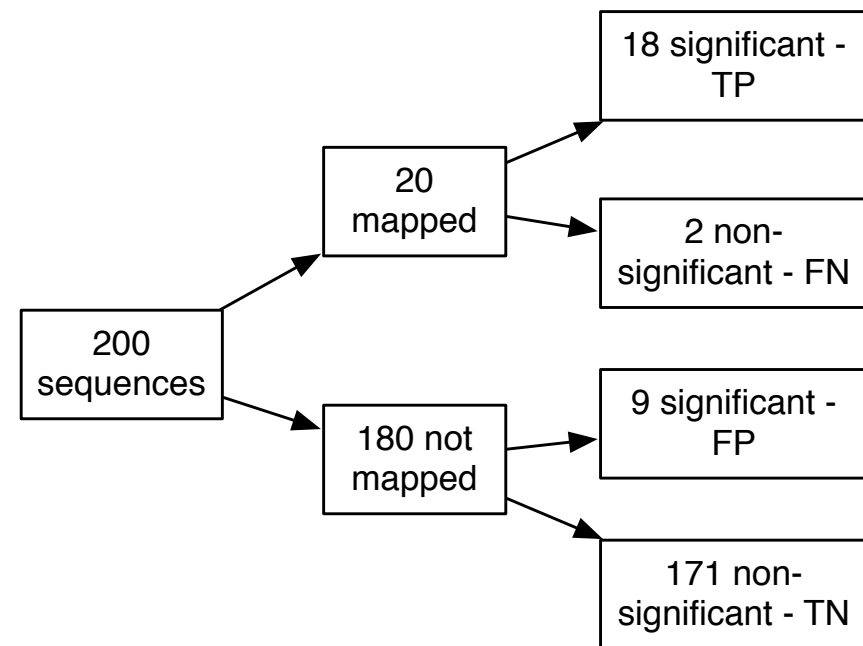
# The False Discovery Rate

The FDR relates to the proportion of errors amongst predictions. It is equal to 1 - precision

False Discovery rate =  $FP/(FP+TP)$



$1/163$



$9/27=1/3$

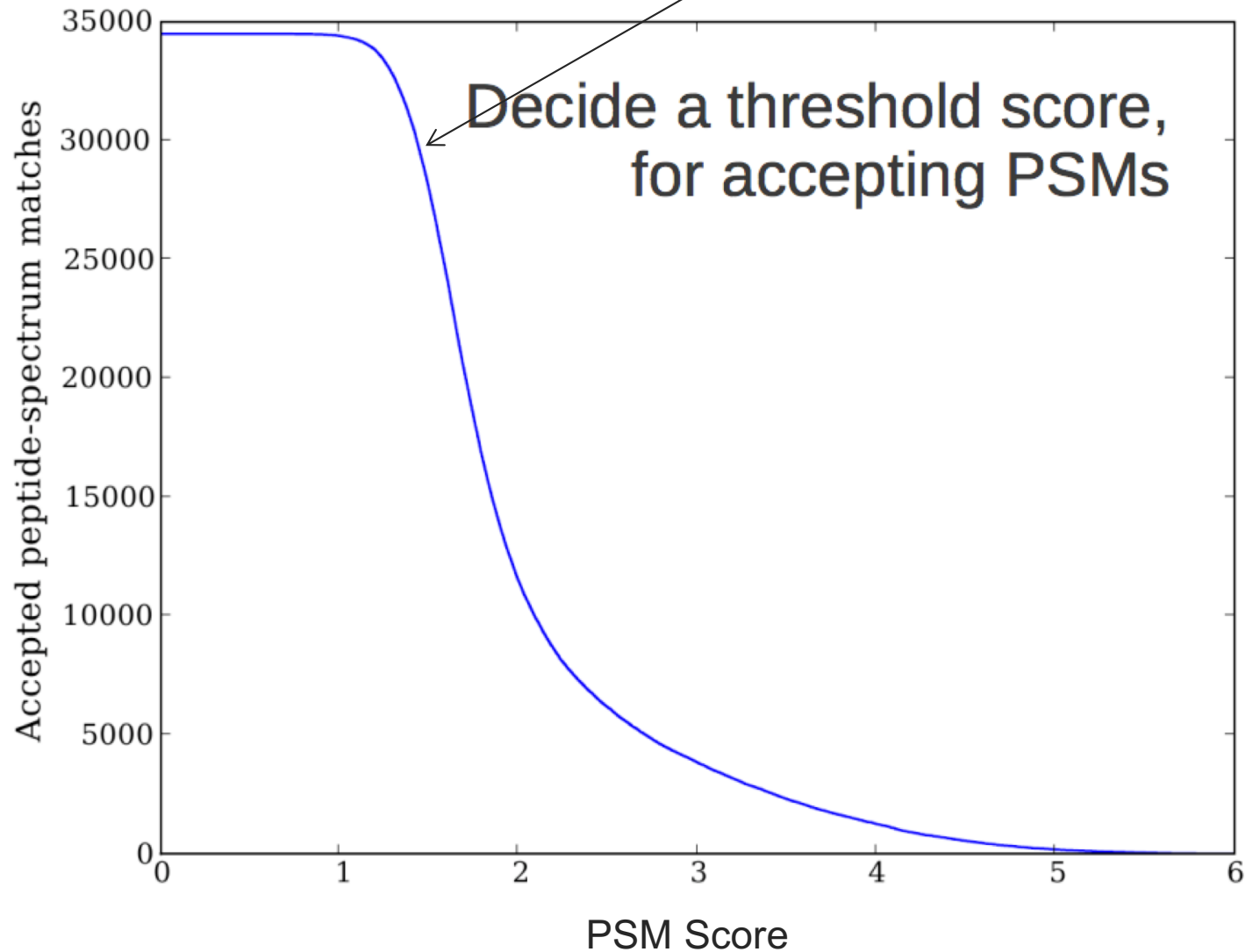
The FDR is sensitive to the proportion of true features in the data.

How to get all the good quality matches?

What if we just use our eye power?

**PSM quality score**

Can do it by eye?



Statistics provides a more objective manner of evaluation

# Statistics help us determine the best match

- p-values
- False Discovery Rate (FDR)
- Posterior Error Probability (PEP)

## The p-value

We can set up our PSMs as a statistical test (based on the following hypothesis statements)

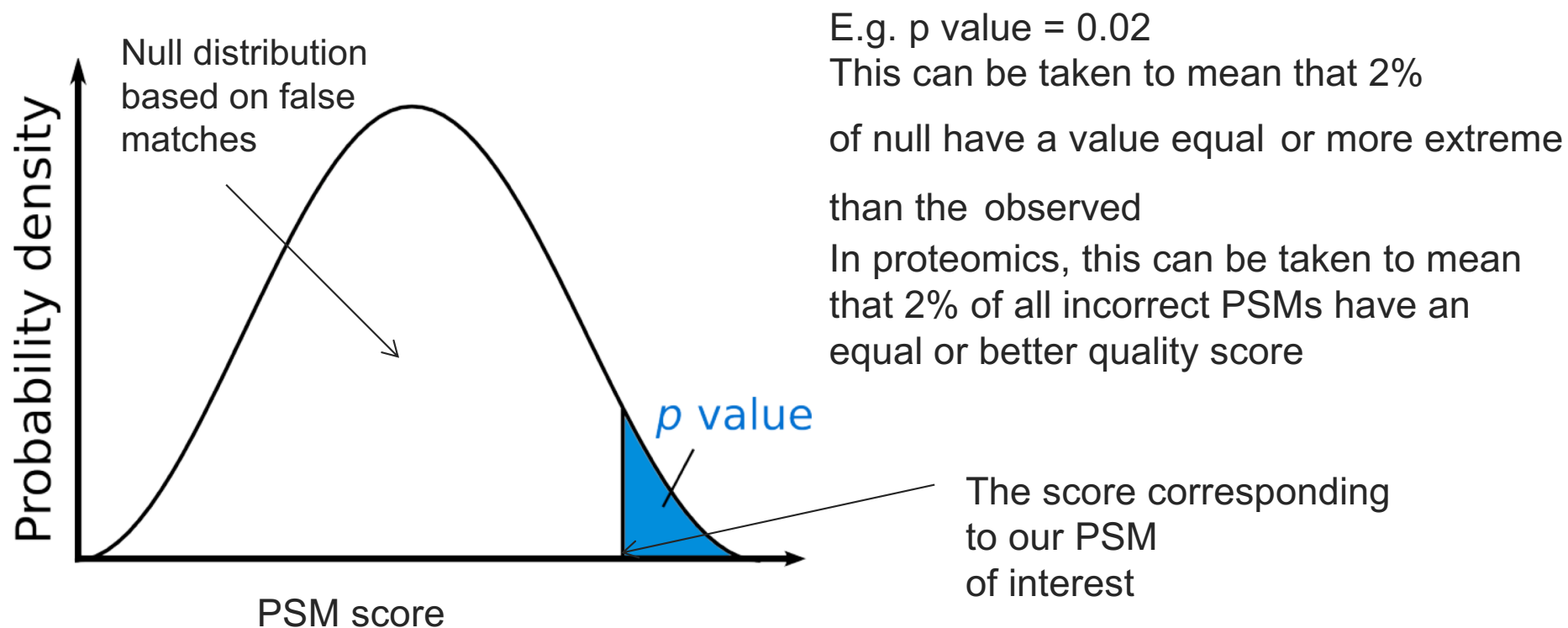
H0: A PSM is incorrect

H1: A PSM is correct

We may reject the null hypothesis with a certain degree of error:

Type I: **Falsely reject the null hypothesis (False positive)**

Type II: Falsely accept the null hypothesis (False negative)



The probability of obtaining an equal or more extreme result, assuming the null hypothesis is true (Type I error)

# The p-value

- We are comparing the observed score against a distribution of “null scores”
- The null distribution are comprised of the natural distribution of values when there is no signal i.e., when a PSM is incorrect (or the null statement is true)
- Why does this make sense?
- Because under this setup, a small p-value would imply that the observed PSM score is very significant (unlikely to arise due to chance).



# The p-value

- For each hypothesis tested. Suppose we use a statistical cutoff at 0.01, we should therefore expect 1 in 100 times the result is a false positive
- Suppose 100 tests are performed, then we should expect  $100 * 0.01 = 1$  false positive
- To control for this, a multiple test correction can be used. For example, to maintain 0.01 FPs given 100 tests, the cutoff can be reduced from 0.01 to  $0.01/100 = 0.0001$

# The p-value (in proteomics)

- Is a **local** measure, meaning that it is confined specifically to the particular PSM under consideration (it is therefore self-contained)
- **Global** measures on the other hand, considers all PSMs scores concurrently and relative to each other (they are therefore not self-contained).
- Lets say we observe a PSM with a score of 1, we can build an empirical reference distribution of similar false/random sequences and find out what are their respective PSM scores. If the observed PSM does better than at least some alpha threshold, then we can say that this PSM is statistically significant, and so we reject the null hypothesis for the alternative.
- This is computationally very intensive. ALSO... what is a reasonable null?

## False Discovery Rate (FDR)

False Discovery Rate (FDR): **The expected fraction of false positives among the significant test statistics. (FP/FP+TP)**

Compare this against the false positive rate which is  $FP/(FP+TN)$

score	type
7.5	correct
7.2	correct
6.9	correct
6.8	correct
6.7	incorrect
6.5	correct
6.4	correct
6.4	correct
6.3	incorrect
6.1	correct
6.0	incorrect
5.9	correct
5.7	incorrect
...	...

Threshold

So how do we look at this?

Let's say we have a set of PSM scores and decide to draw the line at 6, i.e., we accept all PSMs with scores  $> 6$ .

Let's also assume we have perfect knowledge of correct and wrong matches.

We note that 10 PSMs are retained.

Of these, 2 are wrong. So the FDR is therefore

$$FDR = 2/10 = 20\% = 0.2$$

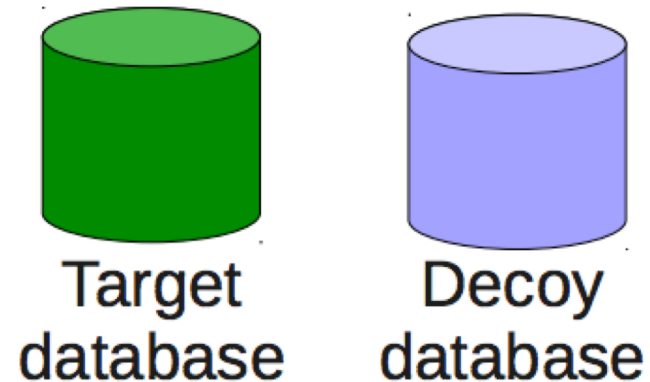
**This seems great. But in reality, we don't know which ones are wrong.**

**This is similar to the null problem in p-value generation. So how do we create something which we know to be wrong or sure?**

False Discovery Rate (FDR)

# The target-decoy analysis

Estimating FDR:  
How to purposely create your incorrect PSMs



## Target database

Protein sequences of the studied organism.

## Decoy database

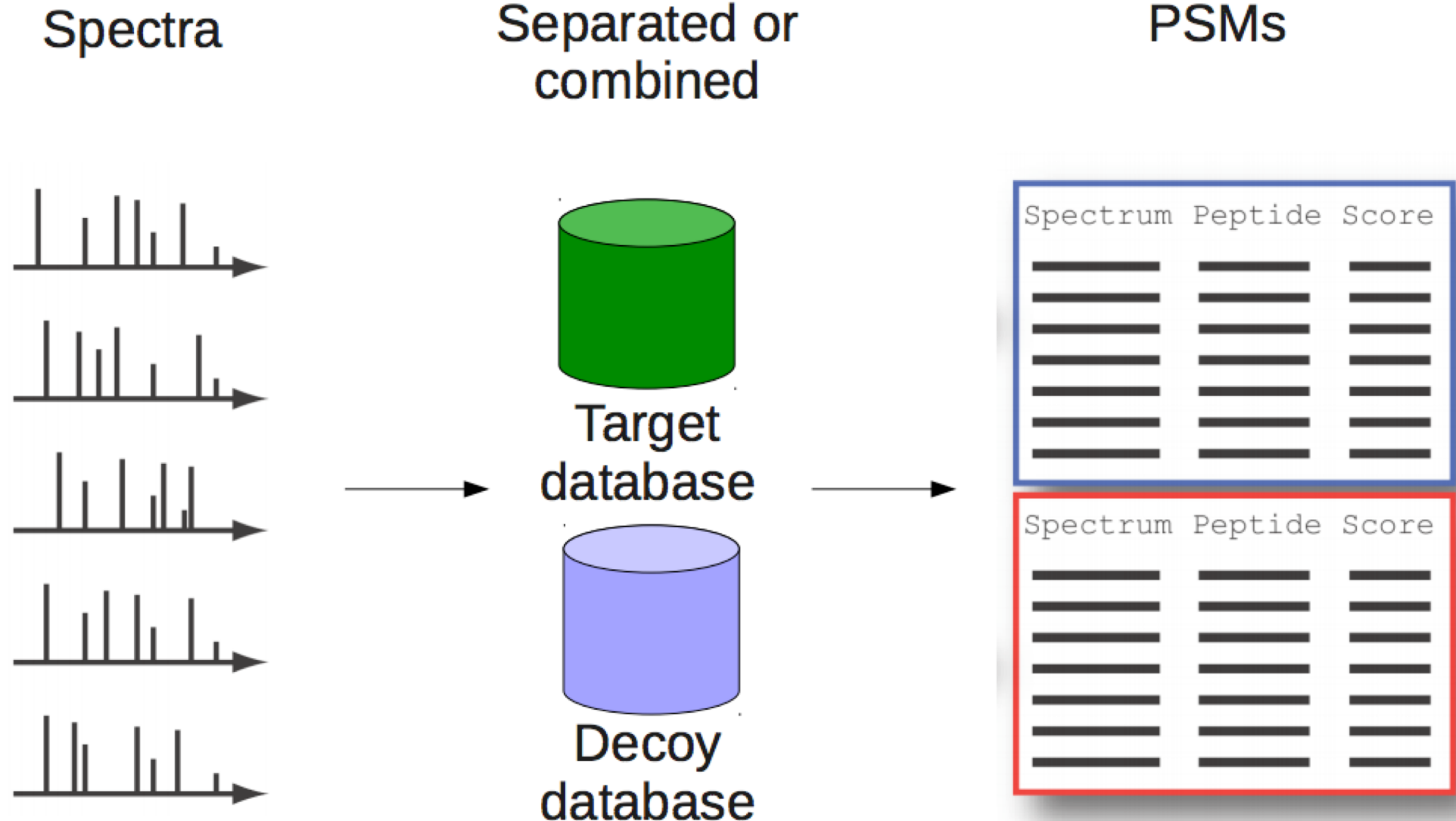
Reversed or shuffled sequences.

## Assumption

Spectra matched to the decoy database are good models of **incorrect** matches to the target database.

In other words, all matches to decoy are false positives

# The target-decoy analysis



### Target-decoy searching steps

- Construct a concatenated target-decoy sequence list, marking decoy sequences with a text flag in their annotation.
- Use a MS/MS search engine to interpret input MS/MS spectra using target-decoy sequence list.
- Evaluate the relative proportion of target and decoy sequences in the search space to derive the multiplicative factor required to estimate false positives, if necessary.
- Estimate false positive-related statistics.
- Use decoy hits to guide the establishment of filtering criteria.
- Report statistics for filtered data set.

### Decoy construction rules

- **Similar** amino acid distributions as target protein sequences.
- **Similar** protein length distribution as target protein sequence list.
- **Similar** numbers of proteins as target protein list.
- **Similar** numbers of predicted peptides as target protein list.
- **No** predicted peptides in **common** between target and decoy sequence lists.

## False Discovery Rate (FDR)

### Reversal

#### Advantages

- Simple
- Preserve general features of the target sequence list e.g. same inter-protein redundancy
- Defined transformation therefore repeatable

#### Disadvantages

- Non-random transformation is less statistically rigorous
- Cannot be used for peptides with low sequence complexity

### Shuffling

#### Advantages

- Simple
- Has desired stochastic properties

#### Disadvantages

- Redundancies and homologies between protein entries will not be preserved, so many more decoy peptides than originally present in the target sequence list

### Random Proteins

#### Advantages

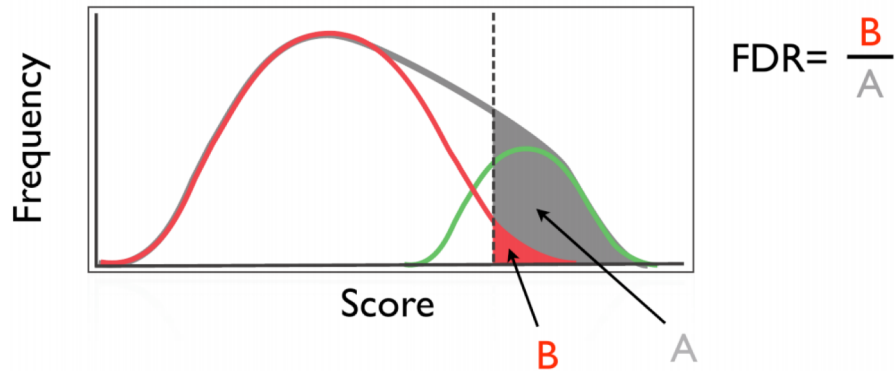
- Has desired stochastic properties
- Can preserve amino acid bias and protein length distribution

#### Disadvantages

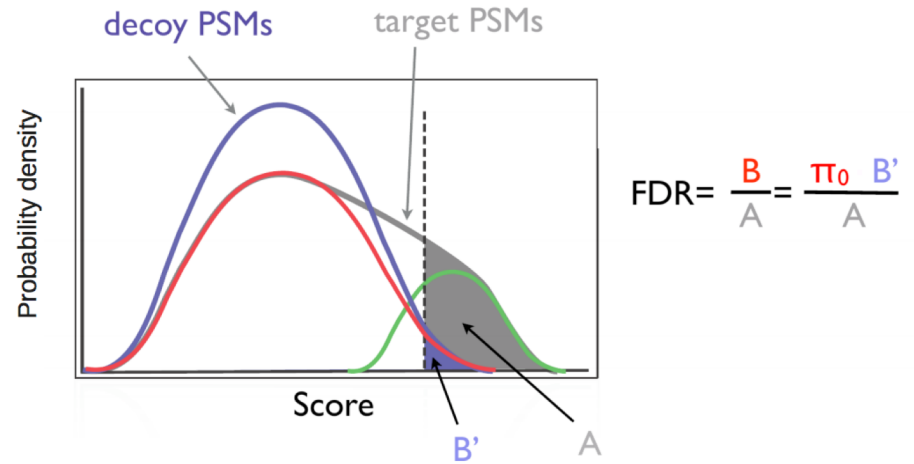
- Redundancies and homologies between protein entries will not be preserved, so many more decoy peptides than originally present in the target sequence list

# FDR estimation based on decoy

No decoy



With decoy



$\pi_0$  is the fraction of incorrect target PSMs among target PSMs

Target-decoy analysis

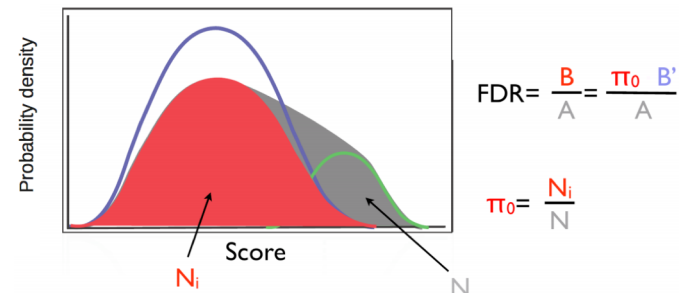
## Combined searches

Target and decoy database are searched together

$$\widehat{\text{FDR}} = \frac{\{\#\text{decoys over threshold}\}}{\{\#\text{targets over threshold}\}}$$

i.e.,  $\pi_0$  is 1

Simpler. Since estimating  $\pi_0$  can be tricky.

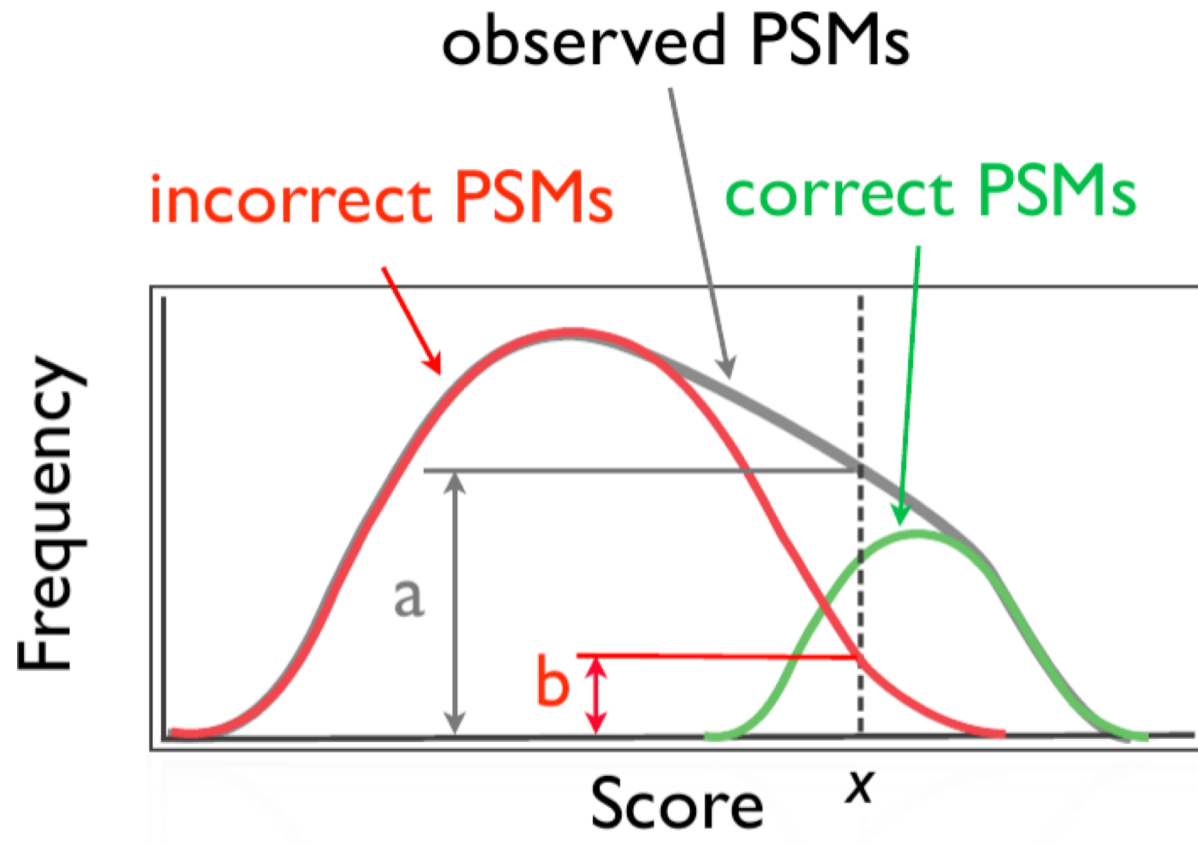


$\pi_0$  is the fraction of incorrect target PSMs among target PSMs



## Posterior Error Probability (PEP)

Posterior Error Probability (PEP): The probability that the null hypothesis is true for a particular test statistic  
In proteomics, it can be taken to mean the probability that a given PSM is wrong.  
PEP is sometimes called “local FDR”

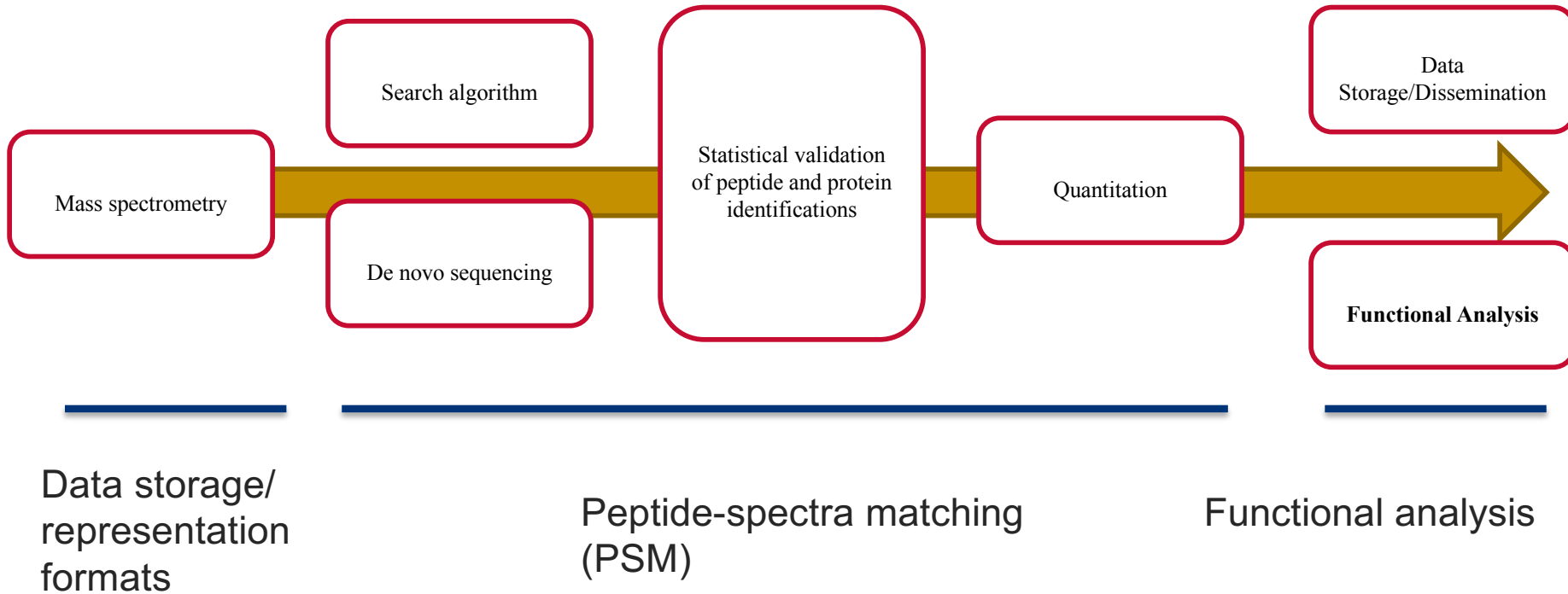


$$\text{PEP} = \frac{b}{a}$$

A PEP is the probability that a PSM scoring  $x$  is incorrect



# Overview of proteo-informatics



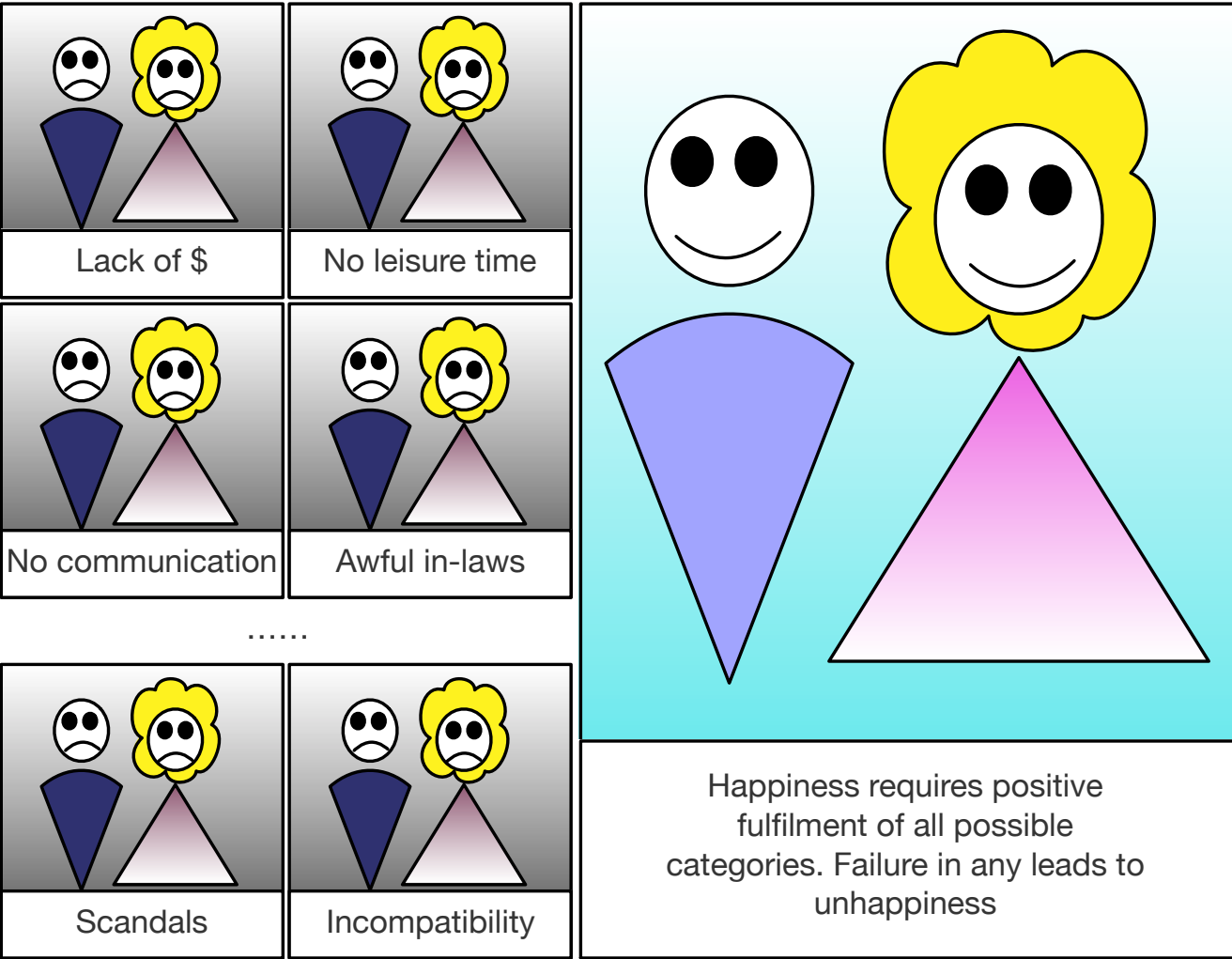
# Functional analysis 1 (Comparative analysis)

- The process of creating knowledge and insight from biological data
- Comparative analysis (group A vs B)
  - Assumption: the differences between two groups are phenotypically relevant and can be used to construct mechanistic explanation
  - This is a fallacious assumption.

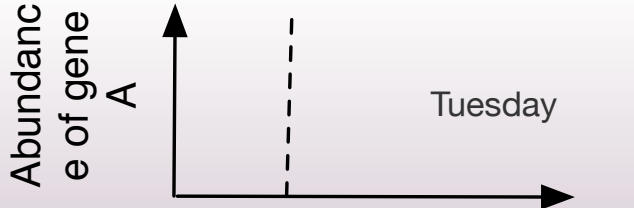
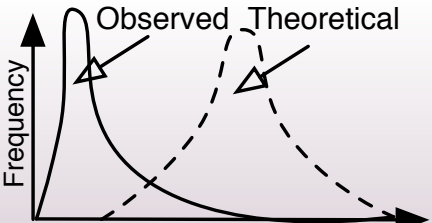

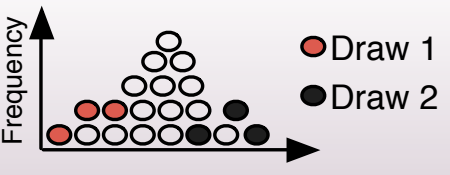
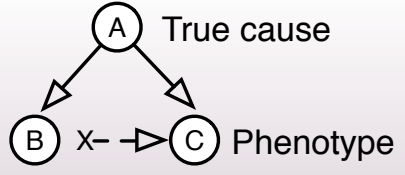
# The Anna Karenina Principle

- Happy families are all alike, every unhappy family is unhappy in its own way  
--- Leo Tolstoy
- Interpreted as: There are many ways to violate the null hypothesis, but only one way that is pertinent to the outcome of interest

# Happiness does not come easy



# Anna Karenina in comparative proteomics

<p><b>False Dichotomy</b>            Null: Gene does not cause disease            Alternative: Gene causes disease</p>	
<p>Wrong test construction</p>	<p>Batch effect</p>
	
<p>Wrong null distribution</p>	<p><b>The gene is relevant</b></p>
	 <p>B is reported but is merely correlated to A</p>
<p>Chance association</p>	<p>Non-causal association</p>

# Dealing with the Anna Karenina

## Causes

- A careless null/alternative hypothesis due to forgotten assumptions:
  - Distributions of the feature of interest in the two samples are identical to the two corresponding populations
  - Features not of interest are equalized/controlled for in the two samples
  - No other explanation for the significance of the test
  - Null distribution models the real world
- These make it easy to reject the carelessly stated null hypothesis and accept an incorrect alternative hypothesis.



# Dealing with the Anna Karenina

## Good Practices to Avoid Wrong Conclusions and Get Deeper Insight

- Check for sampling bias:
  - Are the distributions of the feature of interest in the two samples same as that in the two populations?
- Check for exceptions:
  - Are there large subpopulations for which the test outcome is opposite?
  - Are there large subpopulations for which the test outcome becomes much more significant?
- Check for validity of the null distribution:
  - Is there evidence that suggests the null distribution is inappropriate?
- Check the hypothesis statement construction
  - Are the hypothesis statements being framed correctly (as opposed to a statement that is prone to being rejected for the wrong reasons)?

# Dealing with the Anna Karenina

## Good Practices to Avoid Wrong Conclusions and Get Deeper Insight

- Check your assumptions
  - Are the right assumptions being made (e.g. the independence of measured variables)?
- Check if appropriate summary statistics are used
  - If an event is extremely rare, then using mean/median-based statistics will miss it; ditto if many similar events are present, but only one is relevant
- **Note:** Even if all (or most) of the above points are addressed, it still does not ensure phenotypic relevance, only correlation.

# Functional analysis 2 (Missing proteins)

## Samples

Proteins

nm.3807-S4.xls [Read-Only] [Compatibility Mode] - Microsoft Excel

	A	B	C	D	E	F	G	H	I	J	K	L	M	N	O	P	Q	R	S	T	U	V	W	X	Y	Z	AA	AB	AC
		GeneSy	kidneyTisue1	kidneyTisue2	kidneyTisue3	kidneyTisue4	kidneyTisue5	kidneyTisue6	kidneyTisue7	kidneyTisue8	kidneyTisue9	kidneyTisue10	kidneyTisue11	kidneyTisue12	kidneyTisue13	kidneyTisue14	kidneyTisue15	kidneyTisue16	kidneyTisue17	kidneyTisue18	kidneyTisue19	kidneyTisue20	kidneyTisue21	kidneyTisue22	kidneyTisue23	kidneyTisue24	kidneyTisue25	kidneyTisue26	kidneyTisue27
1	protein	GeneSy	kidneyTisue1	kidneyTisue2	kidneyTisue3	kidneyTisue4	kidneyTisue5	kidneyTisue6	kidneyTisue7	kidneyTisue8	kidneyTisue9	kidneyTisue10	kidneyTisue11	kidneyTisue12	kidneyTisue13	kidneyTisue14	kidneyTisue15	kidneyTisue16	kidneyTisue17	kidneyTisue18	kidneyTisue19	kidneyTisue20	kidneyTisue21	kidneyTisue22	kidneyTisue23	kidneyTisue24	kidneyTisue25	kidneyTisue26	kidneyTisue27
2	P09110	ACAA1	288001.7778	46353.28	237958.5	30102.47	297711.2	37098.09	67454.84	92200.62	231528.4	12617.18	263299.1	NA	222387.2	NA	177211	27857.94	84689.84	43497.89	280540.3	77962.17	235242.5	23827.06	302761.4	41190.07	2064.747	97756.44	122386.3
3	P05166	PCCB	246687.75	70504.27	253890.9	NA	314250.1	33680.65	108554.7	321442.7	260389.5	183399.7	258247.1	192888.5	284934.5	115138	245595.9	30488.41	221565	280540.3	240054.8	65477.99	250479.3	NA	327799	41974.24	125103	321442.7	175808.5
4	Q96RP9	GFM1	37872.59722	NA	40359.89	NA	73975.35	NA	64601.65	56815.28	34506.99	35176.2	98642.34	23060.3	91995.3	NA	37735.48	33491.8	48208.46	47858.24	39584.44	NA	67976.03	23631.74	46763.48	NA	2064.747	53619.99	67555.47
5	Q15417	CNN3	28364.89722	NA	NA	NA	44156.47	52272.02	27128.03	10577.49	32524.27	14171.12	33388.93	27593.38	49821.32	23144.21	24964.95	32403	NA	24907.94	46053.92	NA	NA	25129.86	42948.4	2064.747	26438.35	23207.51	
6	Q96FQ6	S100A16	NA	35176.2	NA	66058.39	NA	30674.6	1804.538	21706.65	NA	11359.64	NA	18677.58	41493.97	12617.18	22496.77	NA	NA	NA	NA	36422.79	NA	75858.83	20589.93	31161.06	2064.747	20398.13	NA
7	P62820	RAB1A	NA	NA	NA	NA	NA	NA	NA	NA	NA	68503.39	NA	NA	NA	NA	NA	NA	NA	NA	32596.28	NA	NA	54839	NA	NA	2064.747	NA	NA
8	P27169	PON1	NA	47101.83	58436.31	18128.35	NA	33573.36	112930.6	NA	NA	NA	59432.1	NA	39084.55	36282.92	16953.34	NA	NA	NA	NA	45107.13	NA	19506.67	NA	38130.55	109838.9	NA	NA
9	Q9UL46	PSME2	33680.65278	99968.93	59047.33	145114.2	33256.26	141575.7	77962.17	75727.38	64365.04	121022.2	40286.83	114480.8	40567.01	104458.4	42876.78	83666.14	55954.92	62742.03	33768.27	111940.8	59915.42	151558.9	38443.16	113145.5	79024.33	73747.38	40140.37
10	P08237	PFKM	39644.09722	NA	54240.61	NA	136064	NA	1804.538	62845.97	141296.3	100616.3	137596.7	NA	140860.9	NA	96590.73	NA	92823.65	51085.24	155550.8	NA	47697.29	NA	136064	NA	2064.747	58610.05	143381.1
11	P04040	CAT	292456.0528	149632.6	239229.2	24964.95	258247.1	220764.4	540115.8	133921.9	284934.5	367784.7	293727.7	179981.9	259314.6	124294.3	204722.1	77070.33	109006.7	136875.9	290924.4	163095.2	237958.5	51389.75	271920.4	227900.3	494422.8	150524.5	294664.3
12	Q8WY46	CTNINB1	NA	NA	NA	NA	NA	1804.538	NA	NA	NA	NA	NA	NA	NA	NA	27646.1	37621.73	26886.24	NA	NA	NA	NA	NA	NA	NA	2064.747	NA	NA
13	Q9H0W9	Cl11orf54	454591.5833	77225.75	393512.7	55431.72	365975.5	180535.1	188742.5	77348.17	352898.9	119242.7	417999.9	263299.1	474797	229655.9	427428	143697	124568	146454.4	441856.5	74156.41	370040.5	44605.86	363784.6	187566.8	129074.8	104101.6	375463.4
14	P31948	STIP1	76018.00556	83236.9	83516.5	137596.7	75613.89	110367.2	98642.34	195146	77709.53	282315.9	65948.94	122386.3	81635.42	129969.2	67749.81	124568	108554.7	135737.2	69039.96	92656.4	85600.47	147792.9	65262.99	109273.7	91127.04	218888	122047.2
15	Q94901	SUN1	57623.33889	NA	NA	NA	7273.86	NA	1804.538	NA	1804.538	NA	58063.49	NA	NA	NA	NA	NA	NA	NA	NA	60013.66	NA	NA	NA	71252.19	NA	2064.747	NA
16	Q99714	HSD17B10	175372.7444	114480.8	181096.8	75400.28	222387.2	91466.47	218888	269679.7	179177.4	165285.9	202618.2	117389.5	191537	41135.21	196208.5	151044.7	210269.6	294964.3	183893	82644.38	179981.9	102286.8	233372.9	91325.89	196996.8	293727.3	174540.8
17	Q15833	STXB2P	14224.84722	24264.99	14303.05	19690.86	16316.33	NA	1804.538	NA	14303.05	17309.98	11459.84	14224.85	12617.18	NA	14224.85	9837.458	21131.38	5634.228	13283.71	28846.59	20057.06	12924.71	17380.49	NA	2064.747	11880.63	13166.66
18	P08195	SLC3A2	50797.625	42825.82	63302.14	26628.24	85345.18	NA	1804.538	NA	7850.17	NA	100616.3	NA	7379.02	NA	7379.02	NA	40191.58	41362.6	72273.86	32198.97	75858.83	NA	2064.747	NA	76292.57	NA	NA
19	P26038	MSN	333342.6833	438752.3	421056.2	381249.5	241992.3	404349.8	164343.5	17022.5	44679.9	117925.5	67779.4	10722.5	44339.9	3517.7	821.2	390317.5	244865.7	273261.7	446678.9	404349.8	306071.8	222387.2	423963.5	191537	182241.6	441856.5	
20	P09104	ENO2	NA	144058.2	NA	184650.5	NA	137596.7	126146.3	21831.59	NA	NA	NA	21950.8	NA	40434.8	NA	5038.25	57080.76	NA	151558.9	NA	181096.8	NA	123793.9	2064.747	NA	NA	NA
21	P07148	FABP1	1219163.714	34579.48	861796.3	NA	940142	NA	1804.538	NA	1130692	NA	1057986	NA	789446.1	NA	221565	NA	NA	NA	1162786	32336.43	805128.4	NA	97005.3	NA	2064.747	NA	1300718
22	Q96Q11	TRNT1	NA	NA	NA	NA	NA	NA	1804.538	NA	NA	NA	NA	NA	NA	NA	NA	37098.09	35565.03	NA	NA	NA	NA	NA	NA	NA	2064.747	NA	NA
23	Q15083	ERC2	NA	NA	NA	85740.42	NA	1804.538	NA	83390.33	NA	NA	NA	NA	NA	NA	NA	142306.8	NA	NA	NA	NA	NA	72396.48	NA	NA	2064.747	NA	70213.43
24	Q15911	ZFH3	NA	NA	178745.3	393512.7	205865.1	682653.9	1804.538	NA	243050.1	NA	189860.5	NA	NA	NA	NA	NA	NA	NA	NA	NA	NA	NA	NA	NA	2064.747	NA	252846.2
25	Q9BUR5	APOU	35479.70278	NA	27260.11	15459.06	40140.37	NA	1804.538	46154.89	30730.15	54737.36	47185.33	13642.38	28517.17	NA	40140.37	NA	10649.17	34436.2	NA	36956.08	16653.18	47858.24	NA	2064.747	33003.64	20057.06	
26	Q9J813	HACL1	417999.9306	NA	435248.4	NA	336790.8	174111.8	276628.6	NA	274264.6	NA	317227.1	271920.4	336790.8	NA	NA	NA	372485.6	446678.9	NA	390317.5	NA	307205	211073.8	2064.747	169817.6	333342.7	
27	Q8WUW4	POCD6P	50008.50556	34991.44	75054.27	50108.55	59047.33	41611.18	84319.78	97140.59	56715.96	134561.7	61533.77	67555.47	65262.99	68597.03	59827.38	73200.35	75049.44	64108.37	40359.89	70903.29	49636.31	49821.32	37258.59	76579.02	76685.11	37386.23	
28	P53597	SUCLG1	387432.1583	99433.59	228946.3	94932.09	310472.5	150524.5	187002.3	299487.5	275420.7	308775.7	299487.5	101732.7	245595.9	108554.7	270810.9	89524.72	192915.6	276628.6	357417.6	96737.9	205171.6	95793.82	288001.8	162300.5	193664.8	299487.5	245595.9
29	Q00186	STXB3P	NA	28468.21	NA	NA	19019.68	1804.538	NA	191949.8	NA	NA	NA	NA	21949.83	NA	NA	NA	NA	NA	NA	15575.29	29005.53	NA	NA	NA	2064.747	NA	NA
30	Q8N335	GPDI1	52415.71111	NA	59328.51	NA	54240.61	21949.83	109383.8	91466.47	45427.61	109273.7	50443.03	NA	52700.48	23221.01	45502.32	NA	57623.34	41362.6	54737.36	NA	62380.69	NA	54839	23827.06	71658.52	49636.31	
31	P08621	SNRNP70	48594.65	51791.05	47269.07	86082.28	44306.32	53026.19	1804.538	NA	59432.1	54839	49636.31	60065.33	52477.21	NA	72977.35	74546.25	82242.07	33003.64	60605.33	49636.31	93224.91	NA	56917.54	2064.747	NA	50797.63	
32	Q969V6	MKL1	NA	91325.89	55954.92	NA	74269.09	80102.57	1804.538	NA	71906.43	NA	152627.3	72497.5	72497.5	89662.88	51690.71	68707.95	41576.85	72021.55	92973.8	NA	NA	NA	NA	88904.66	2064.747	NA	NA
33	P08311	CTSG	NA	NA	46154.89	NA	NA	67879.78	1804.538	NA	53026.19	NA	NA	68927.99	NA	218057.1	78414.15	NA	NA	NA	NA	46895.88	NA	NA	NA	56514.53	66379.24	NA	NA
34	Q9JKU7	ACAD8	46053.91944	31797.32	50179.16	NA	64601.65	NA	75160.02	49228.15	44010.16																		

## Missing proteins

- Any gene sequence whose respective protein has never been observed is an MP.
- Alongside various initiatives---e.g. GPMDB, PeptideAtlas and neXtProt --- the goal is to establish a genome-proteome bridge.

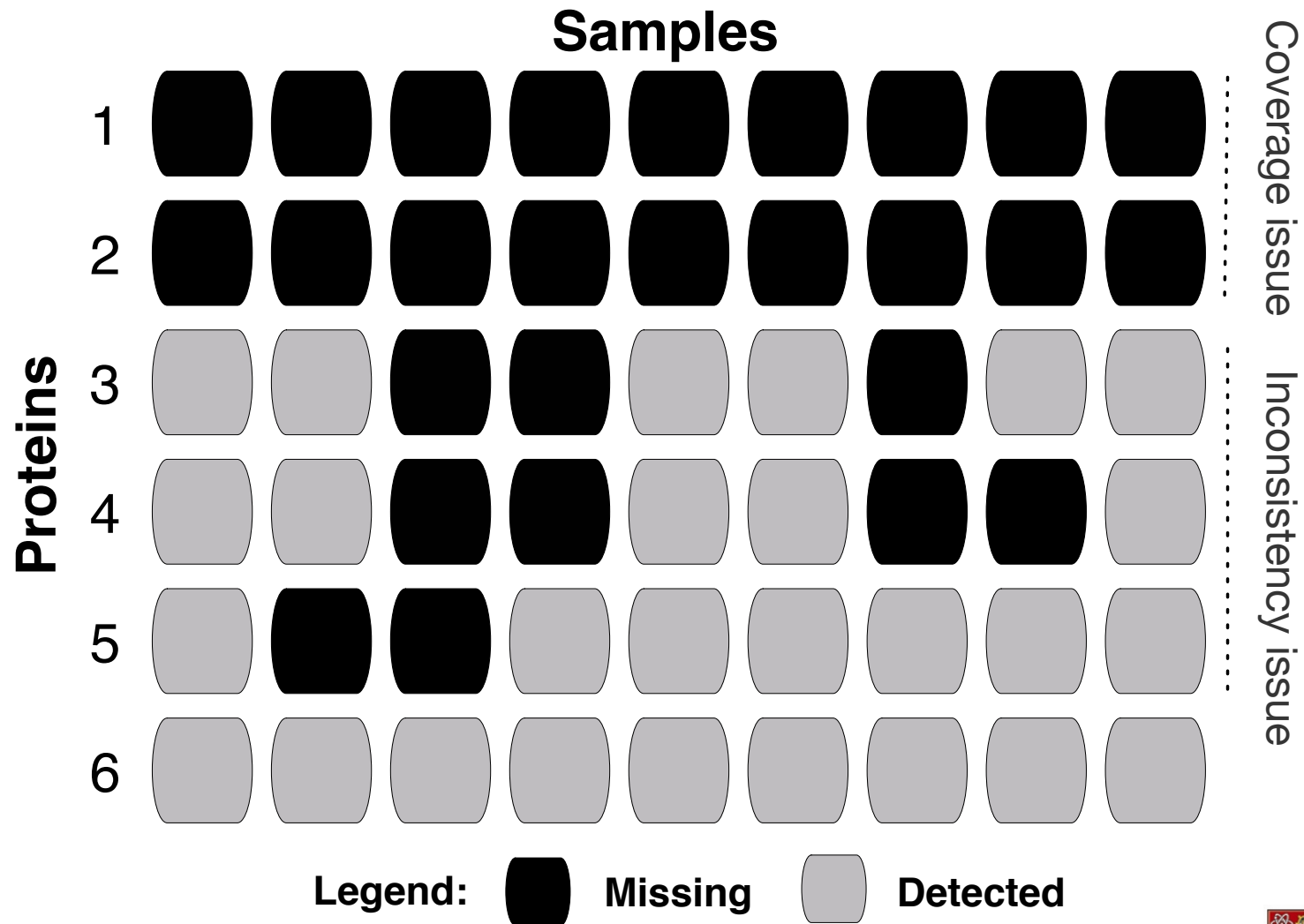
# Missing proteins (Tiers 1 to 5)

PE Tier	Inclusion criteria	Percentage of proteome against 20,055 proteins	Notes
1	Evidence at proteome level	~82.0% (16,518)	*At least 2 unique non-overlapped peptides at least 9 amino acid residues long
2	Evidence at transcript level only	~11.5% (2,290)	*The transcript must be confidently detected, but no corresponding protein evidence
3	Homology inference only	~3.0% (565)	*Inferred homologues without protein or transcript support
4	Predicted	~0.5% (94)	*Predicted coding sequence, without homology, transcript or protein support
5	Dubious	~3.0% (588)	*The sequence may not fully meet the criteria for a predicted coding sequence *Uncertainty over the veracity of the coding sequence (i.e., we do not know the sequence is correct) *Some studies do not consider PE5 as MPs

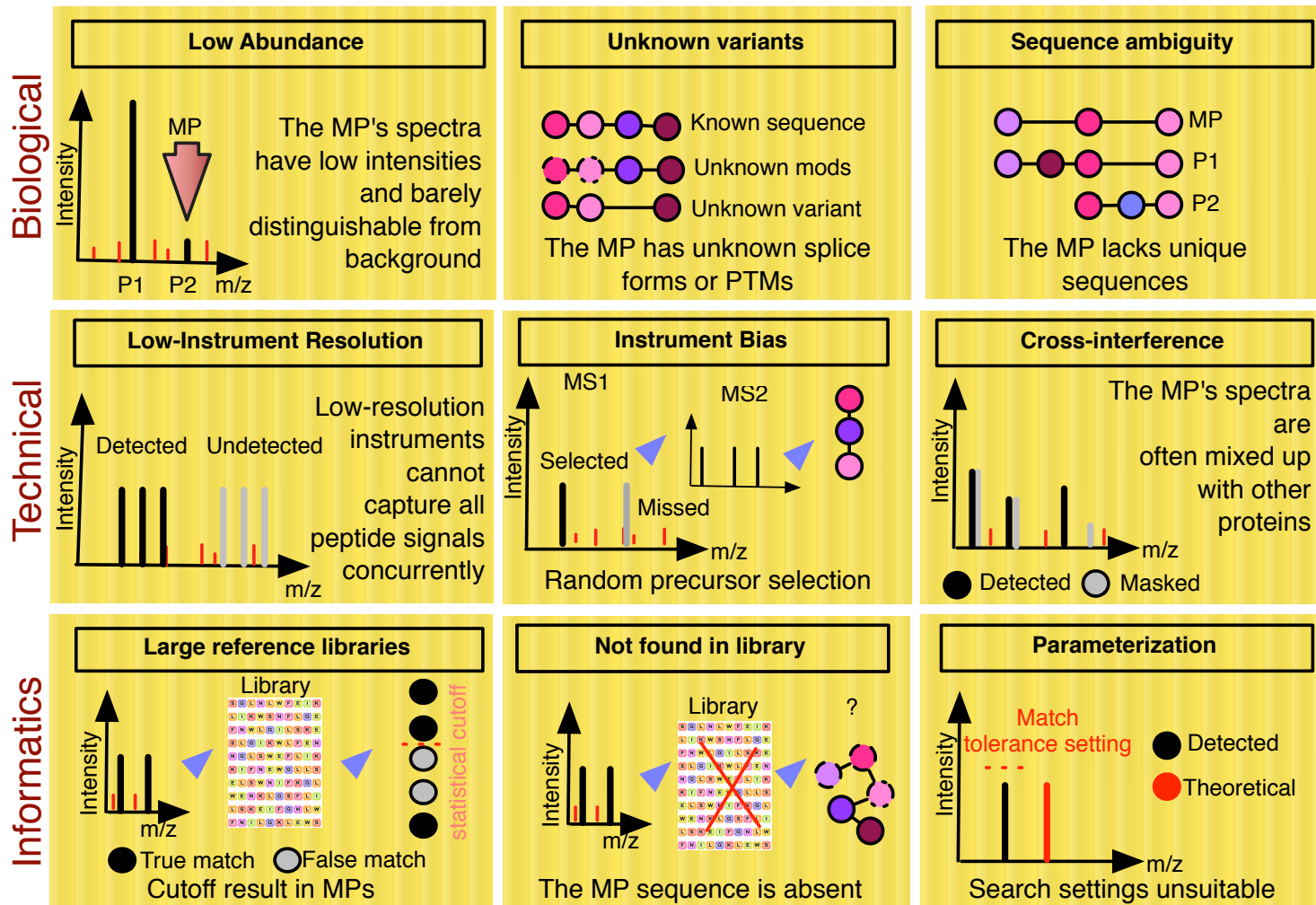
# Missing proteins and relations to coverage, consistency problems

- An MP may be one of the following
  - sequence is known but hard to detect,
  - sequence is known but never detected in MS
  - sequence is not known but evidence exists for it e.g. via gene prediction or in raw spectra.
- The “missing-protein problem” (MPP)---viz. the difficulty in detecting certain proteins despite transcript or theoretical evidence---should more rightfully be considered a narrow manifestation of the more general coverage (the inability to survey the entire proteome) and consistency (the inability to consistently detect a protein) problems

# Coverage and consistency



# Why do proteins go missing?

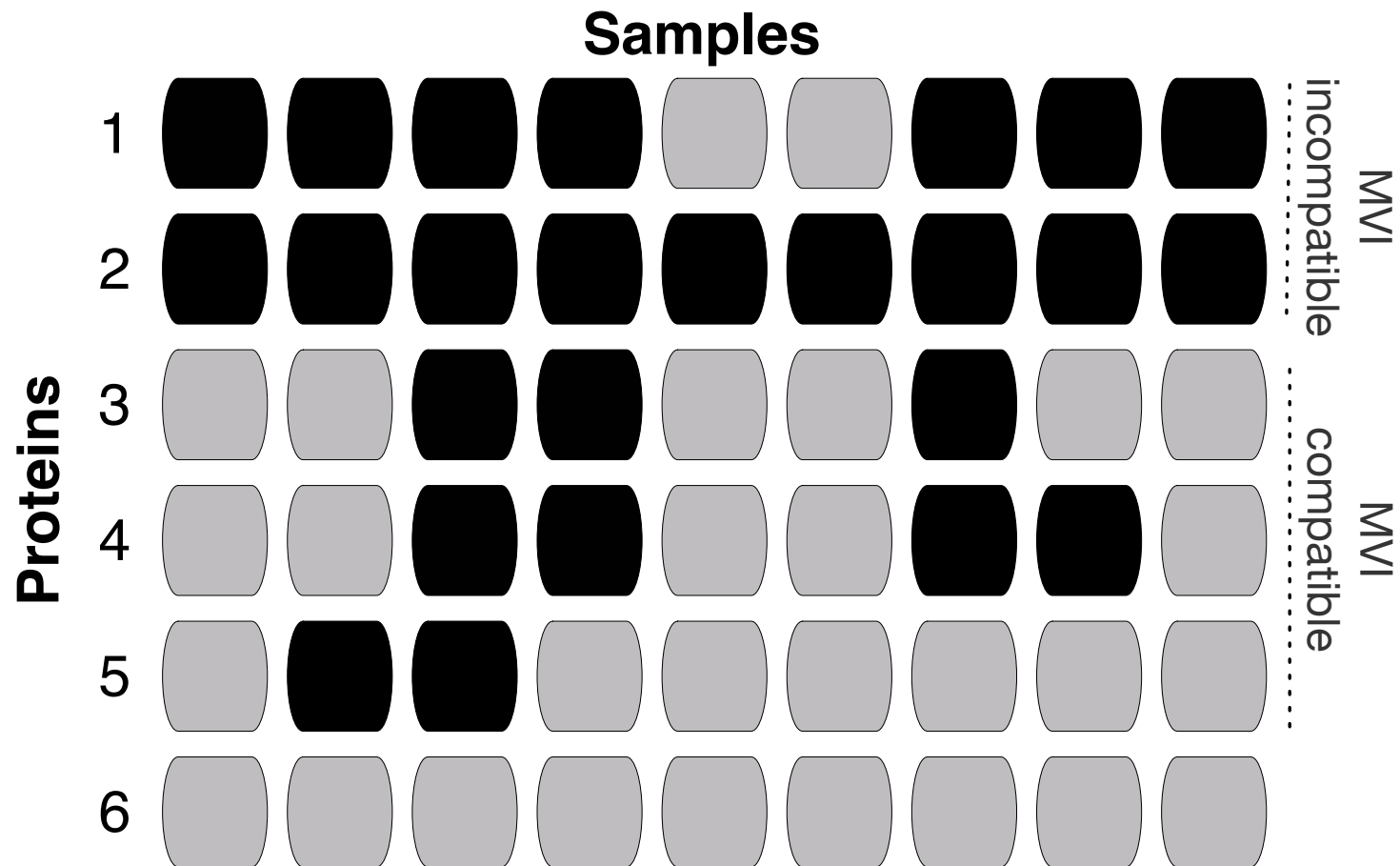




# Missing value imputation (MVI)

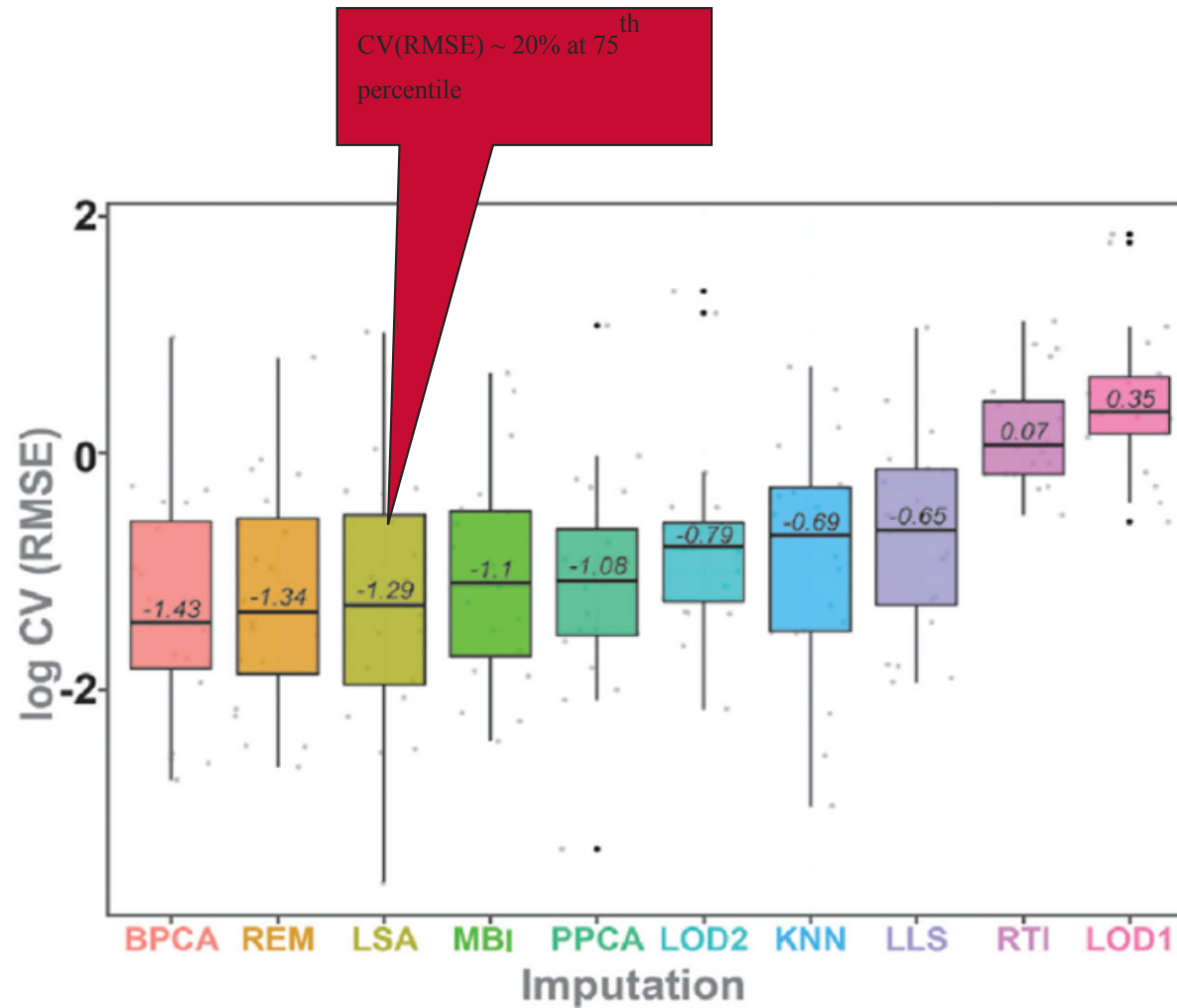
- A few strategies:
  - We fill in 0s or a fixed value based on the average of all protein expression
  - For each missing value per protein, we fill in the average value based on all observed values for that same protein
  - We estimate the missing value based on proteins that are known to be correlated

# Missing value imputation (MVI)



Limitation: It mostly only works well for inconsistency issue

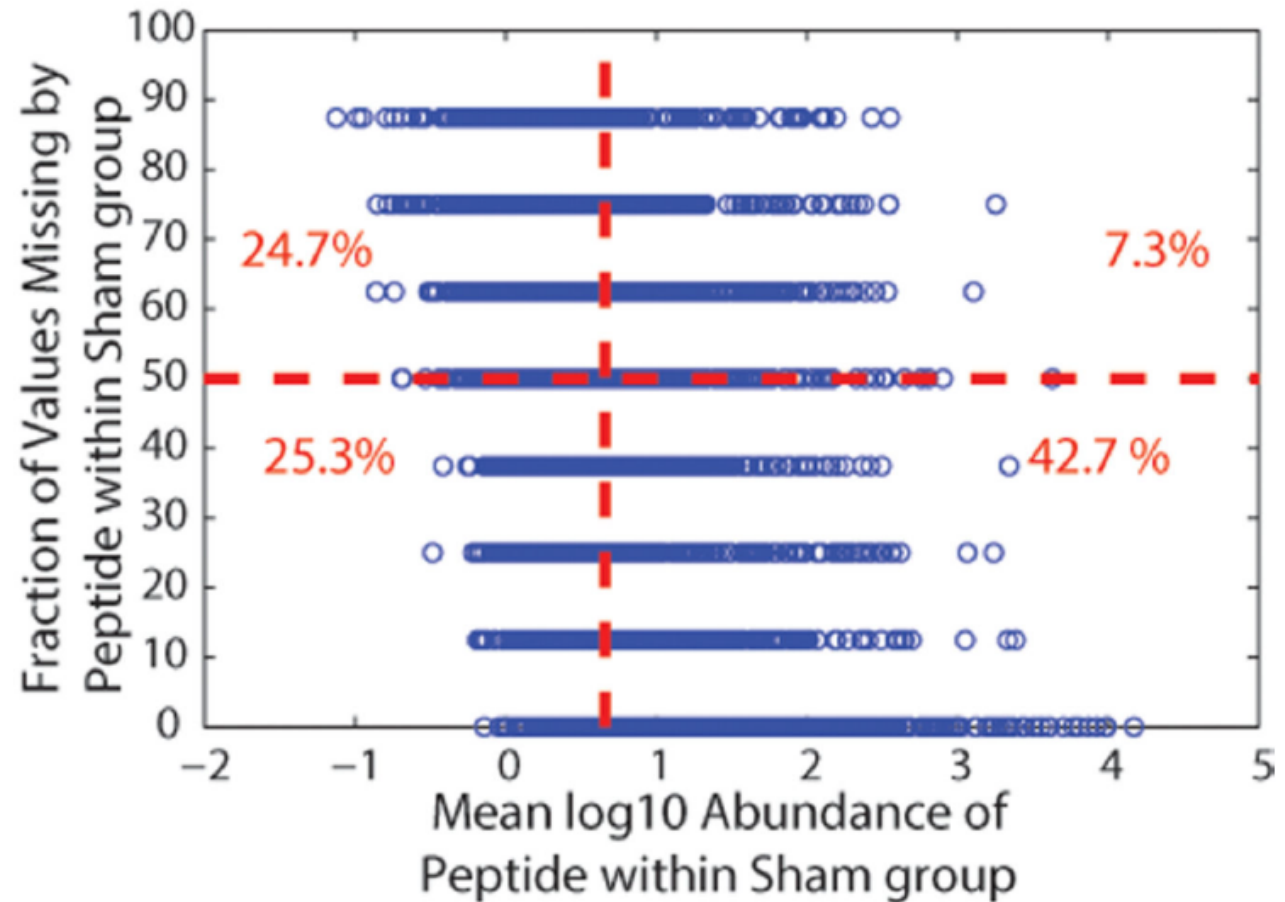
**MVI  
methods  
really  
don't  
work very  
well**



**Figure 2.**

Boxplot of the average  $\log_{10} CV(RMSE)$  for the imputed dilution series datasets (Table 1) at the (A) peptide and (B) protein levels. The lower line represents the 25th percentile, the upper line of the box represents the 75th percentile, and the inner line corresponds to the median  $\log_{10} CV(RMSE)$ .

**High abundance has lower % of MPs. However, low abundance is not a solely explanation. The MPs are equally distributed across the horizontal median.**



**Figure 1.** Average  $\log_{10}$  intensity as measured by peptide peak area in the control group versus fraction of missing values and peptide counts associated with bins corresponding to the fraction of missing data comparing phenotypes and exposures for datasets from (A) human plasma and (B) mouse lung. The control group for the human plasma is the normal glucose tolerant (NGT) samples, and the sham group for the mouse lung is the regular weight mice with no lipopolysaccharide (LPS) exposure. The vertical red line represents median average intensity, and the horizontal red line represents the point that 50% of the values are missing.

# How about we use the idea of “guilt-by-association?”

- **Postulate:** The chance of a protein complex being present in a sample is proportional to the fraction of its constituent proteins being correctly reported in the sample

- Suppose proteomics screen has 75% reliability; a complex comprises proteins A, B, C, D, E; and screen reports A, B, C, D only but not E.

⇒ Complex has 60% ( $= 0.75 * 4 / 5$ ) chance to be present

⇒ The unreported protein E also has  $\geq 60\%$  chance to be present, as presence of the complex implies presence of all its constituents

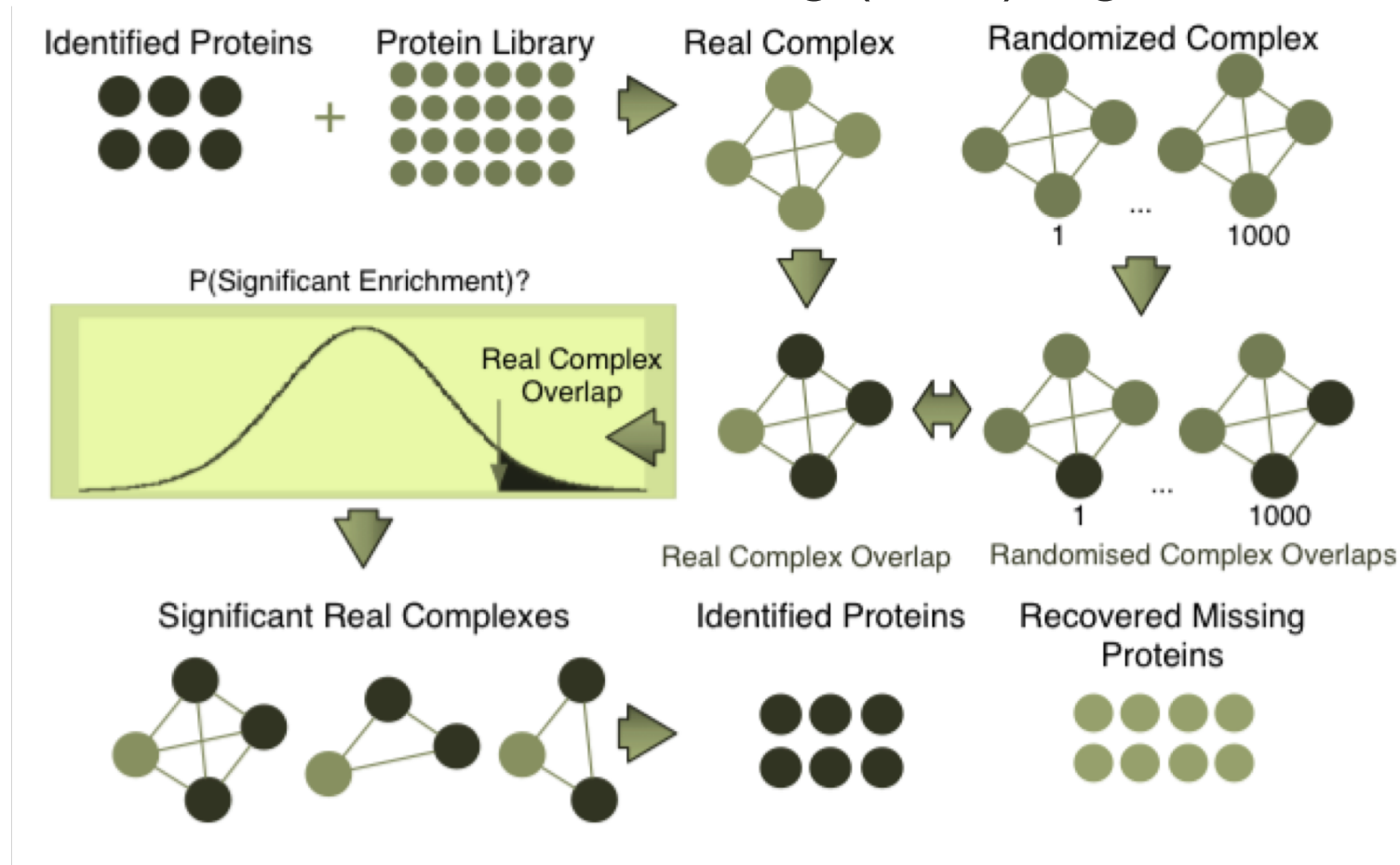
⇒improving coverage (recover missing proteins)

⇒ Each of the reported proteins (A, B, C, and D) individually has 90% ( $= 100\% * 0.6 + 75\% * 0.4$ ) chance of being true positive, whereas a reported protein that is isolated has a lower 75% chance of being true positive

⇒removing noise

# How about we use the idea of “guilt-by-association?”

The functional class scoring (FCS) algorithm



# Does context really work?

Method	Novel Suggested Proteins	Recovered proteins	Recall	Precision
PEP	1037	158	0.317	0.152
Maxlink	822	226	0.454	0.275
FCS (predicted)	638	224	0.450	0.351
FCS (complexes)	895	477	0.958	0.533

- Looks like running FCS on real complexes is able to recover more proteins and more accurately

But we can't rank the individual proteins simply based on p-values. Can we do better? This is a story for another time. Or simply refer to <https://www.comp.nus.edu.sg/~wongls/talks/wls-incob2017.pdf>

## What have we learnt?

- Getting good quality PSMs requires consideration of a large number of factors
- The p-value, FDR and PEP are used as statistical approaches for different purposes
- There are 3 strategies for creating decoy libraries in FDR estimation
- Proteomics is plagued with coverage and consistency issues, requiring various rescue analysis



## You should be able to

- Describe the various factors affecting PSM quality
- Describe p-values, FDR and PEP
- Describe and evaluate the various decoy library generation strategies (sequence reversal, sequence randomization) for FDR estimation
- Describe coverage and consistency issues in proteomics

# Readings

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